



# Fairness Benchmarking of MACs

Harmen R. van As, Günter Remsak, Jon Schuringa

Vienna University of Technology, Austria

# Goal and Content

---

**Goal:** Find algorithm to determine the maximal individual node throughputs while bottleneck-link fairness is fulfilled

## Content

- Two definitions for bottleneck fairness
- Corresponding fairness algorithms and examples
- Two traffic scenarios

# Local Fairness Definitions

---

- 1 Flow rates on bottleneck are proportionally reduced by the total amount of offered traffic for that bottleneck link
- 2 Flow rates on bottleneck are proportionally reduced by the total number of connections on bottleneck link

# Definitions

---

## Given:

- Number of nodes  $N$
- Requested rate from node  $i$  to node  $j$   $r_{i,j}$

## Calculated:

- Flow on link  $i$   $f_i$   
Sum of all requested rates passing link  $i$
- Number of demands passing link  $i$   $nd_i$
- Remaining capacity on link  $i$   $rc_i$   
Link capacity minus the sum of all allowed rates passing link  $i$
- Allowed rate from node  $i$  to node  $j$   $ar_{i,j}$   
Rate calculated by the algorithms

# Algorithm for Fairness Definition 1

---

**Set:**  $rc_i=1$ ;

**Step 1:** for all links: calculate flow on link  $i$ :  $f_i$

**Step 2:** if  $(rc_i/f_i < 1)$  // condition for a bottleneck

take always the highest overloaded bottleneck:  $\min(rc_i/f_i)$

bottleneck link: indicated by index  $b$

else  $ar_{i,j} = ar_{i,j} + r_{i,j}$ ; stop;

**Step 3:** for all flows passing this bottleneck set:  $ar_{i,j} = rc_b / f_b \times r_{i,j}$  and  $r_{i,j} = 0$

**Step 4:** calculate remaining capacities  $rc_i$  of all links; goto **Step 1**;

# Algorithm for Fairness Definition 2

---

**Set:**  $rc_i=1$ ;

**Step 1:** for all links: calculate flow on link  $i$ :  $f_i$

**Step 2:** if  $(rc_i/f_i < 1)$  // condition for a bottleneck

take always the highest overloaded bottleneck:  $\min(rc_i/nd_i)$   
bottleneck link: indicated by index  $b$

else  $ar_{i,j} = ar_{i,j} + r_{i,j}$ ; stop;

**Step 3:** for all flows passing this bottleneck:

if  $(rc_b/nd_b > r_{i,j})$

$ar_{i,j} = r_{i,j}$ ;  $nd_b = nd_b - 1$ ;  $r_{i,j} = 0$ ;

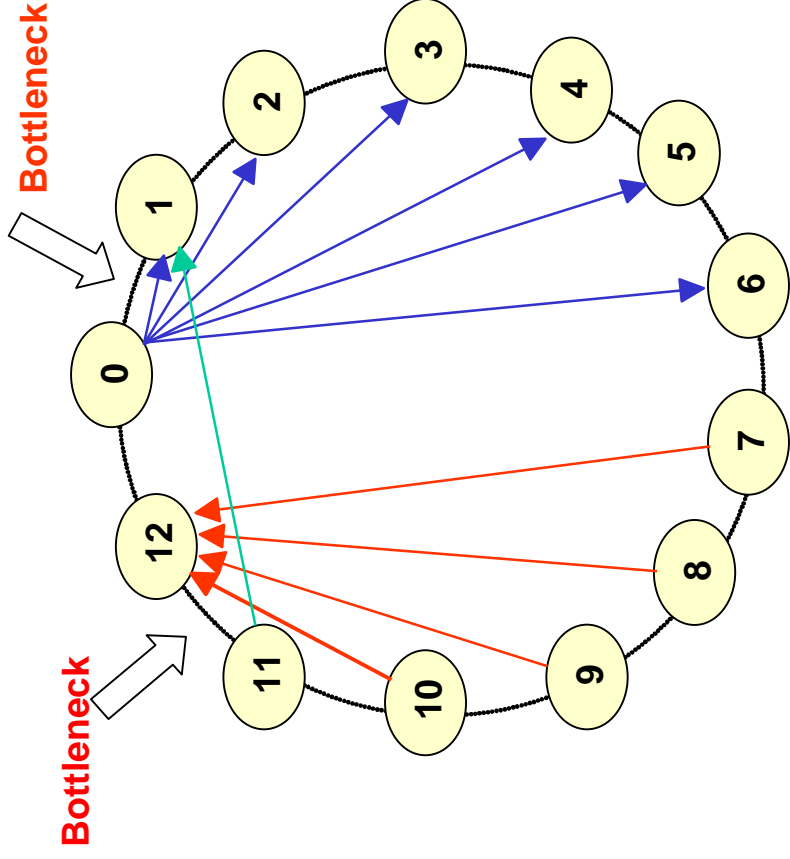
calculate remaining capacities  $rc_i$  of all links;

goto **Step 1**;

else  $ar_{i,j} = rc_b/nd_b$ ;  $r_{i,j} = 0$ ;

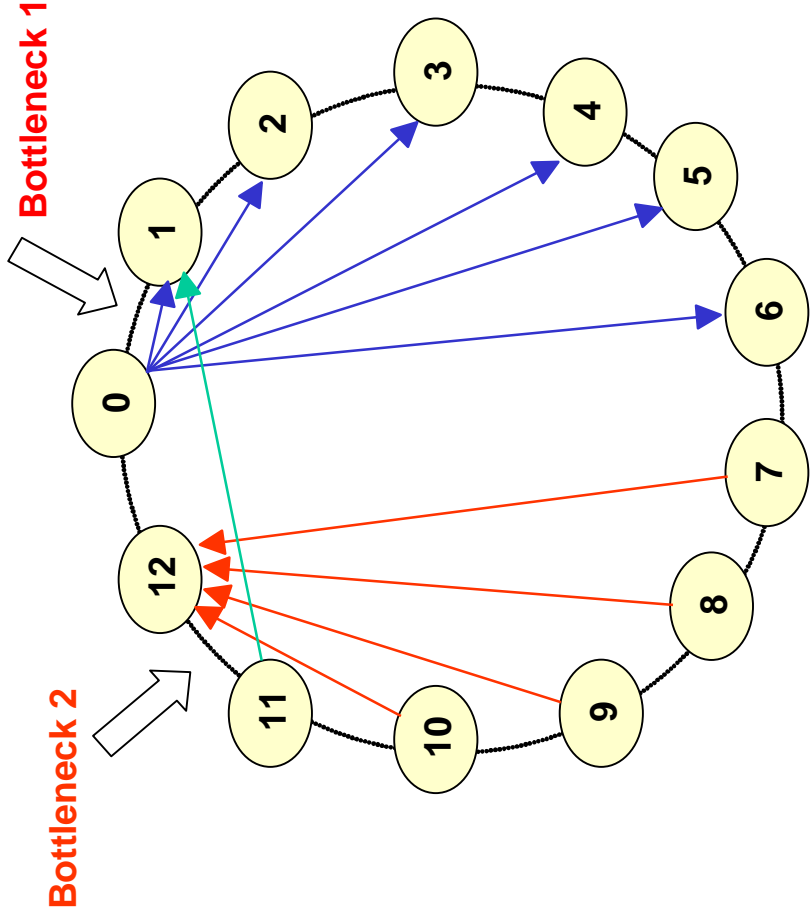
**Step 4:** calculate remaining capacities  $rc_i$  of all links; goto **Step 1**;

# Example: Fairness Definition 1



Source	Sink	Rate	Fair
0	1	0.01	0.01
0	2	0.01	0.01
0	3	0.01	0.01
0	4	0.01	0.01
0	5	0.01	0.01
0	6	0.01	0.01
7	12	0.1	0.071
8	12	0.1	0.071
9	12	0.1	0.071
10	12	0.1	0.071
11	1	1	0.71

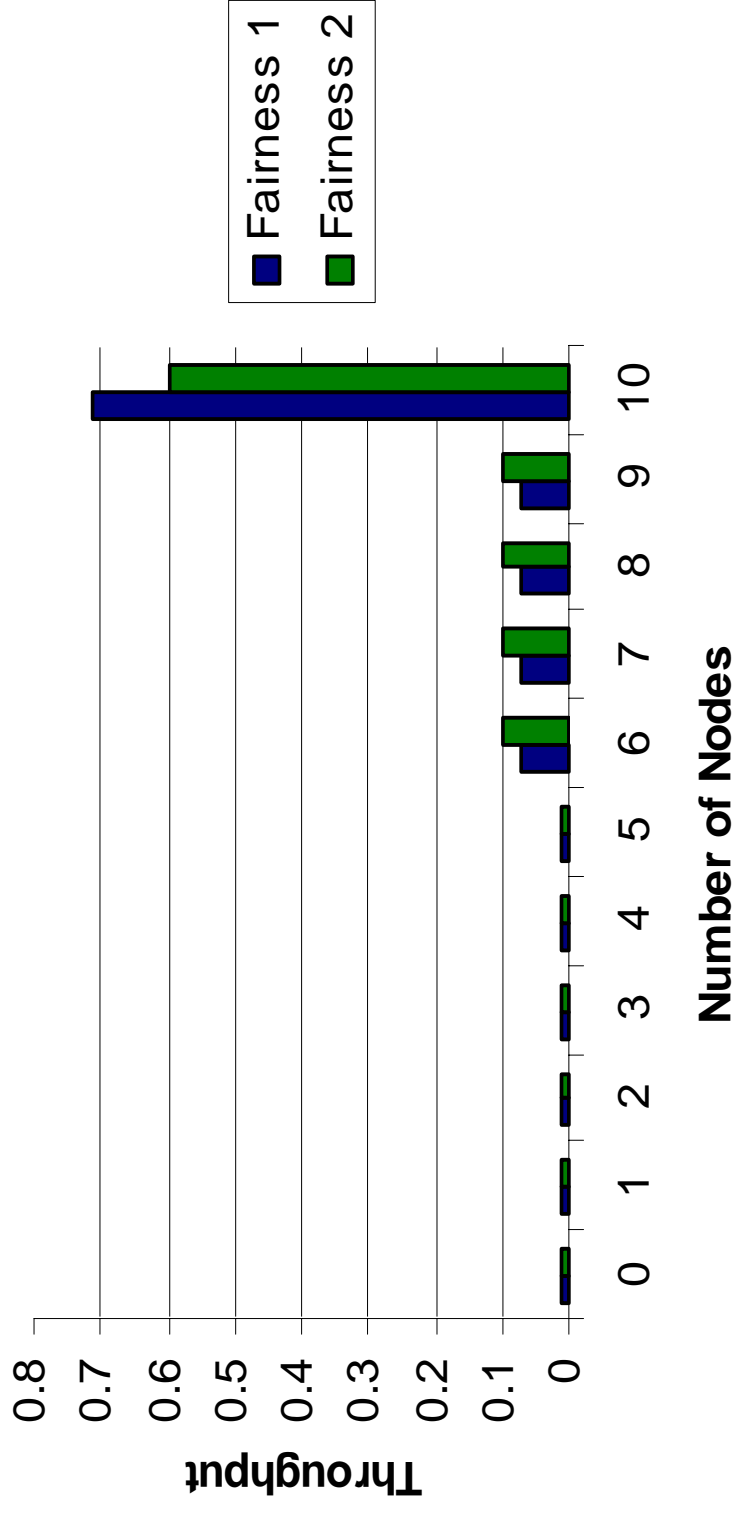
# Example: Fairness Definition 2



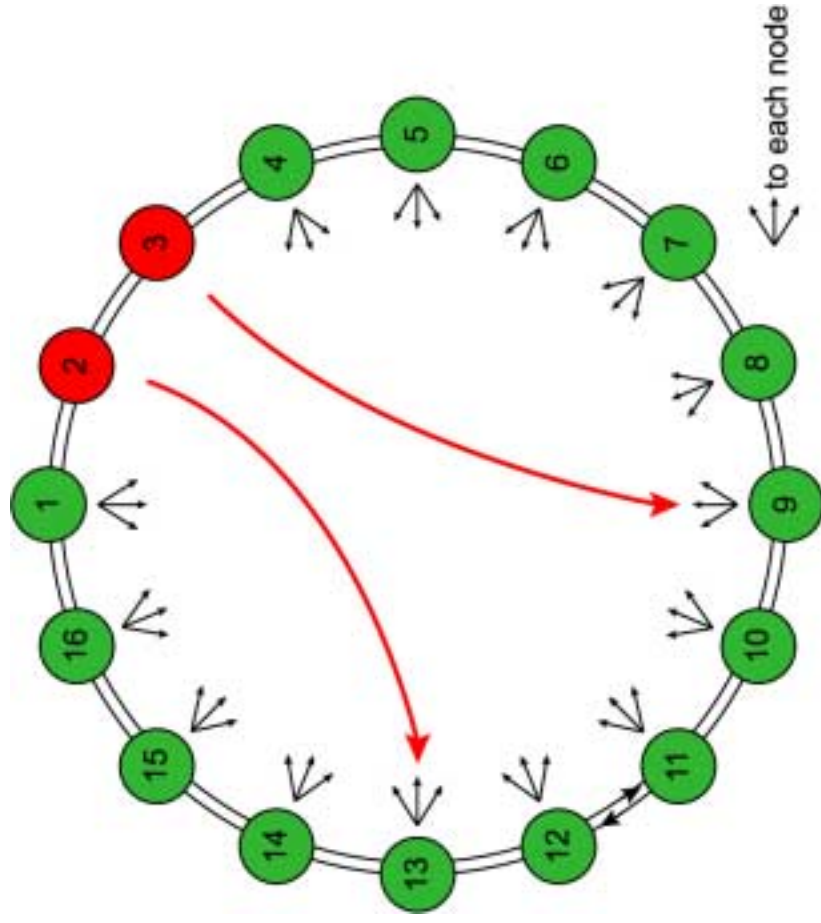
Source	Sink	Rate	Fair
0	1	0.01	0.01
0	2	0.01	0.01
0	3	0.01	0.01
0	4	0.01	0.01
0	5	0.01	0.01
0	6	0.01	0.01
7	12	0.1	0.1
8	12	0.1	0.1
9	12	0.1	0.1
10	12	0.1	0.1
11	1	1	0.6



# Throughput



# Scenario 1

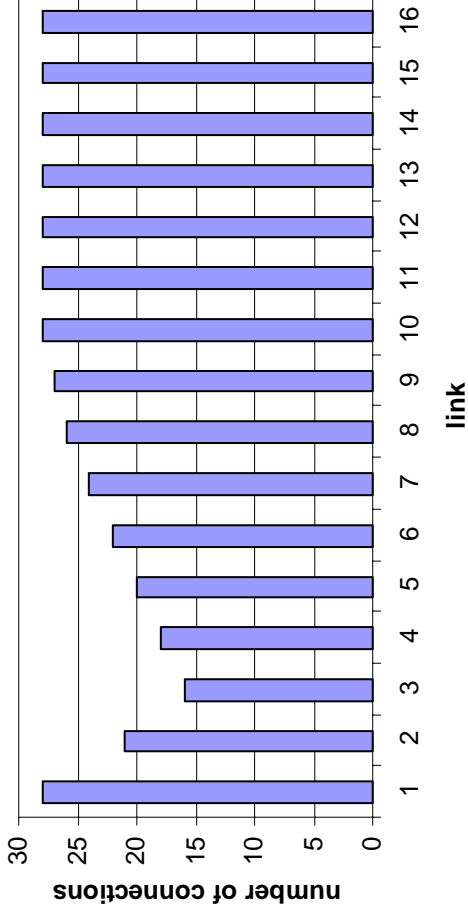


Uniform traffic  
Saturated sources  
16 nodes

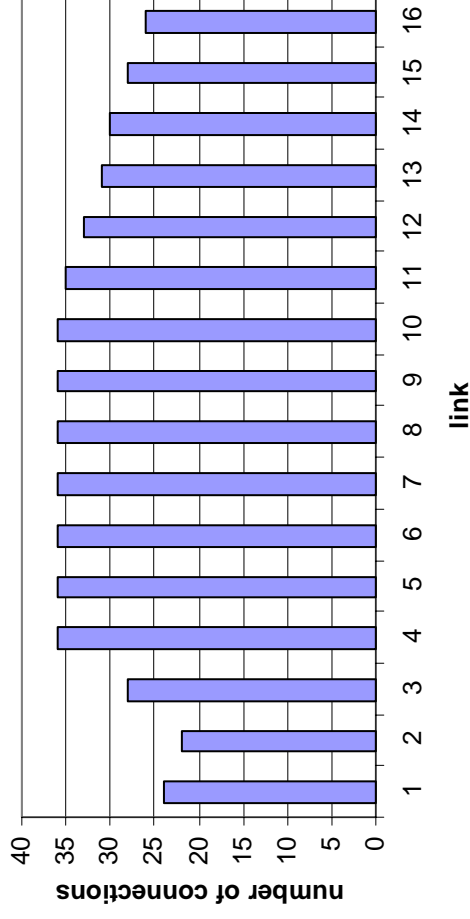
# Number of Connections per Bottleneck Link

## Scenario 1

### Ring 0



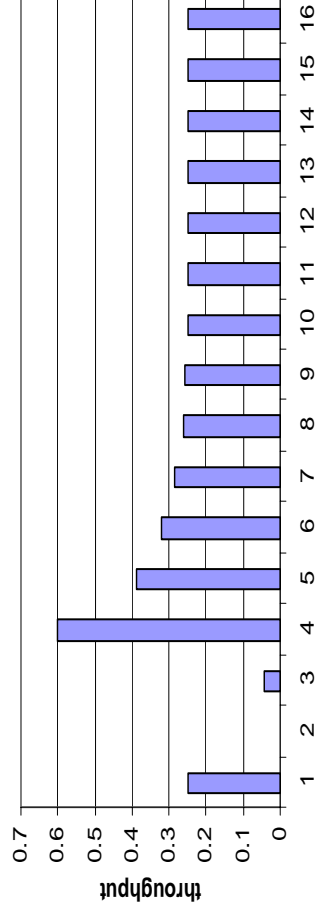
### Ring 1



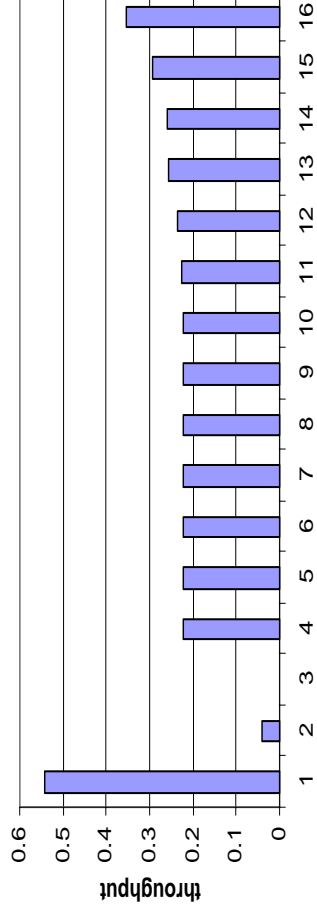
# Throughput per Node

## Scenario 1

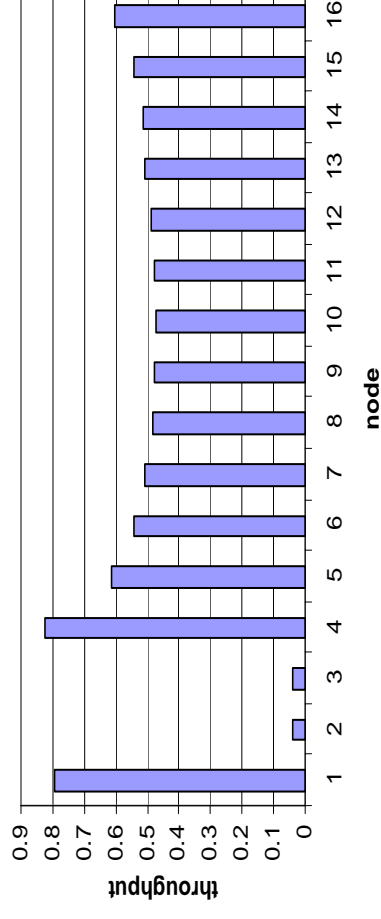
### Ring 0



### Ring 1



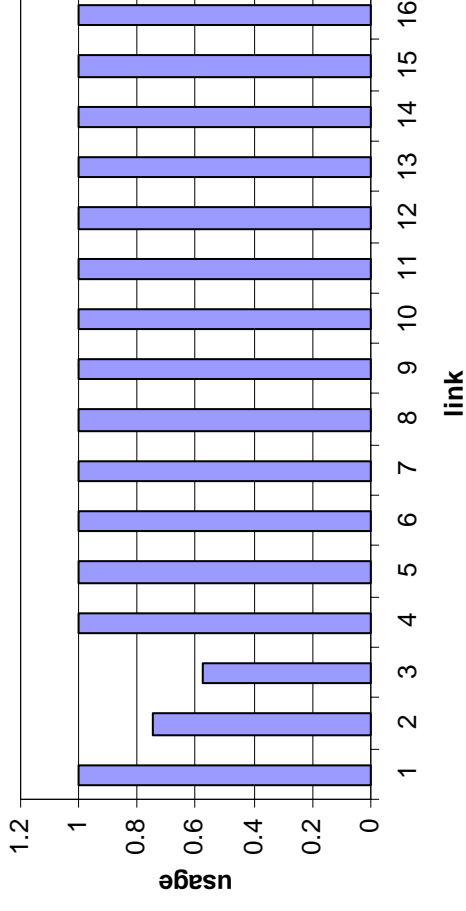
### Ring 0 + Ring 1



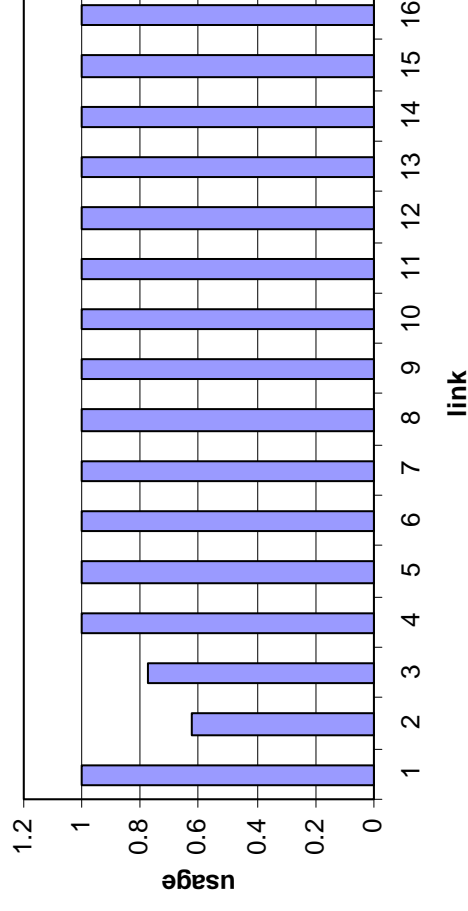
# Link Usage

## Scenario 1

### Ring 0



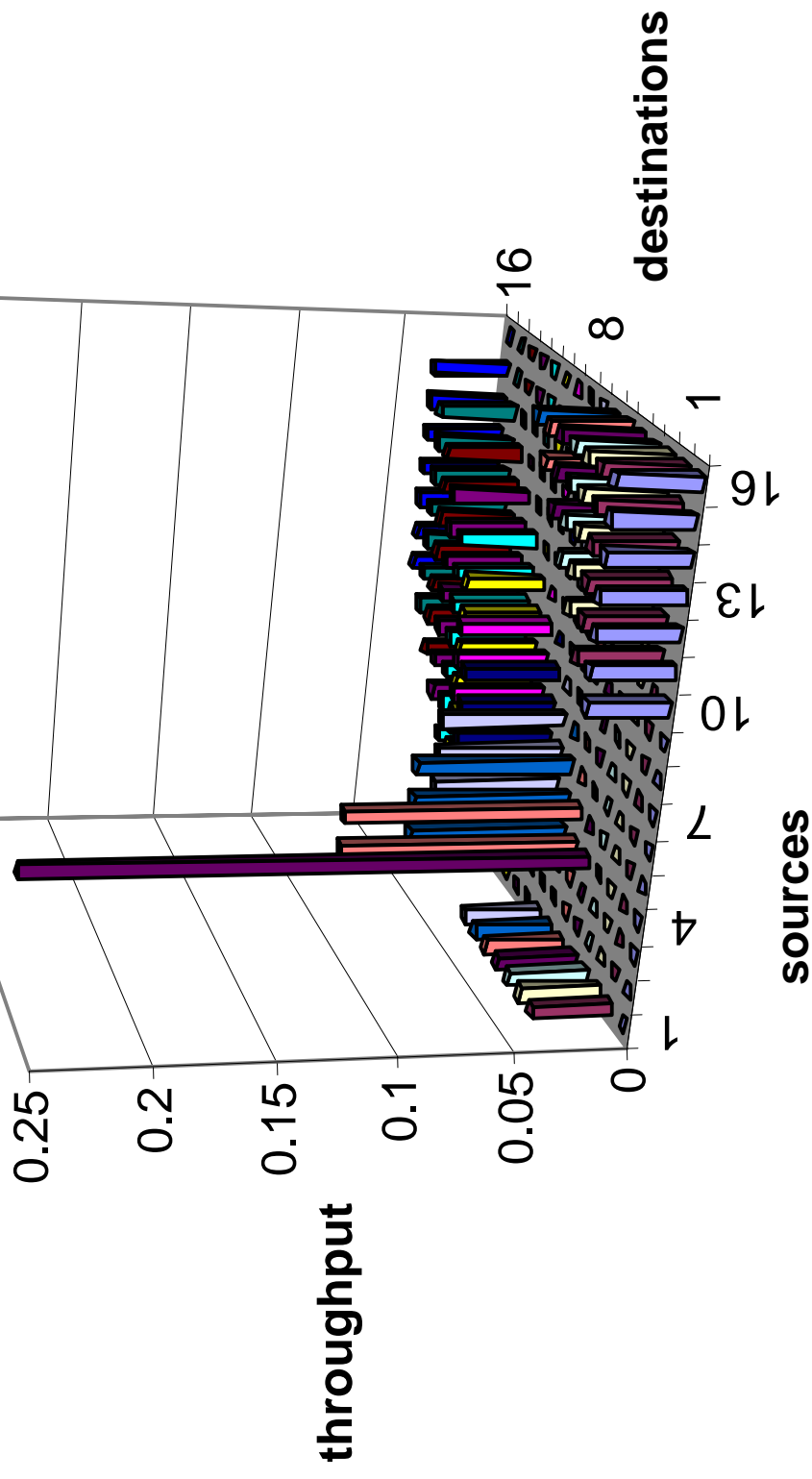
### Ring 1



# Throughput per Source/Destination Pair

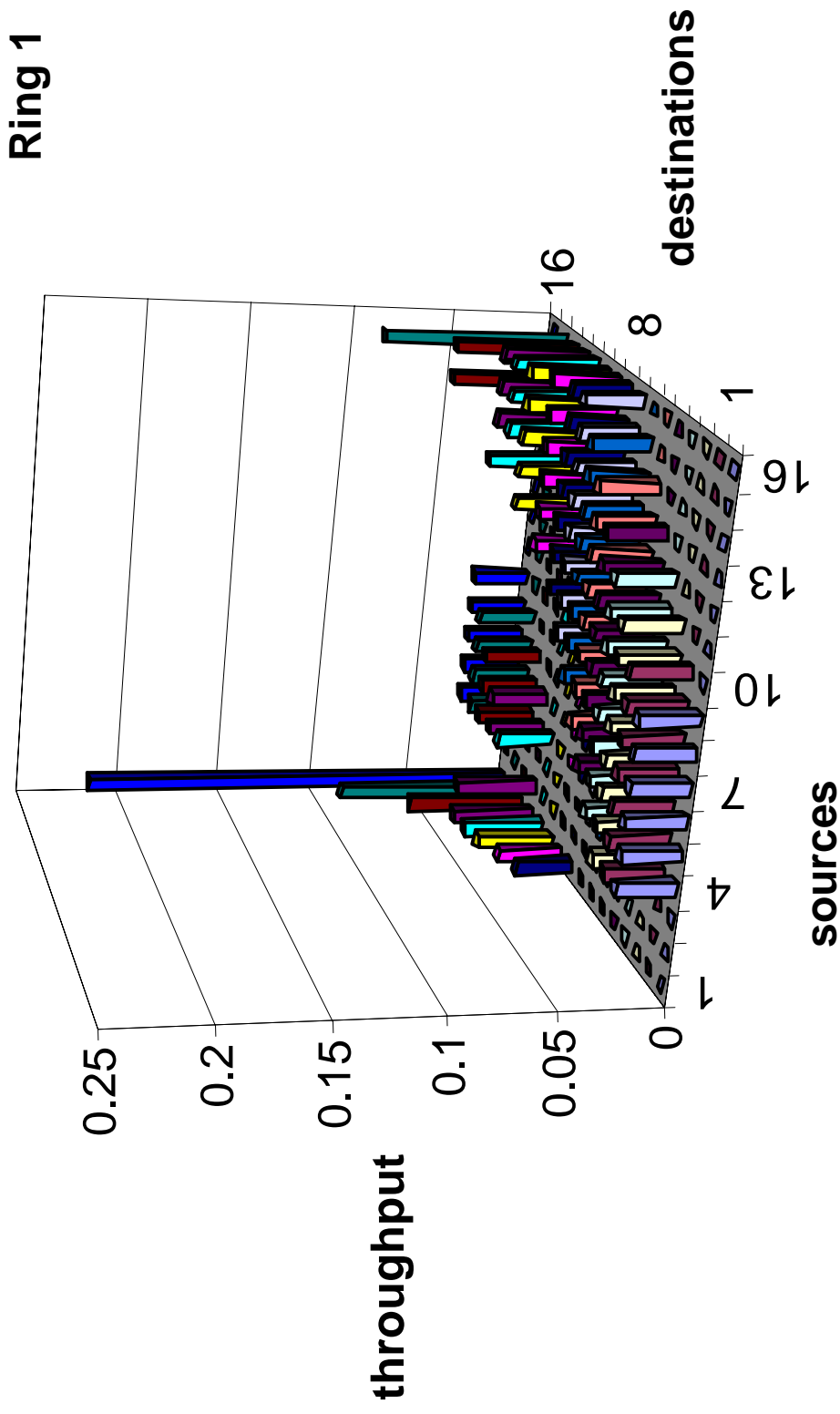
Scenario 1

Ring 0

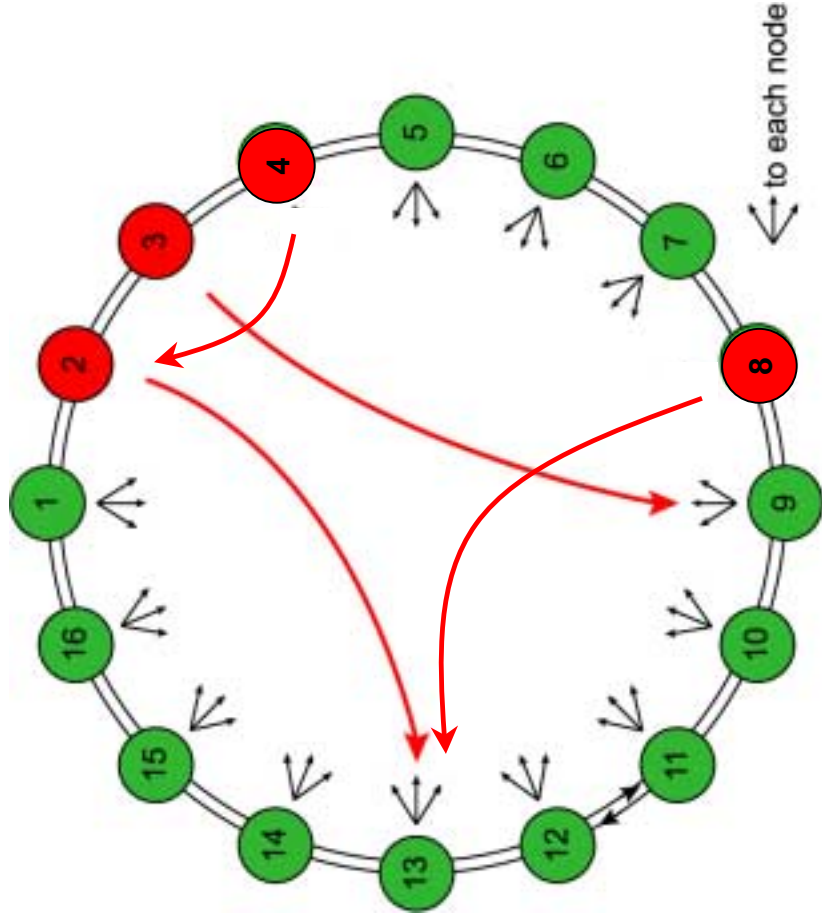


# Throughput per Source/Destination Pair

Scenario 1



# Scenario 2

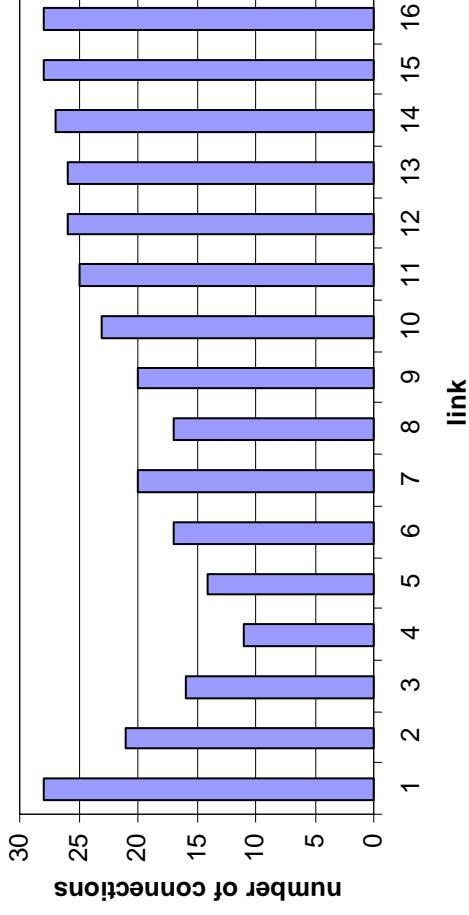


Uniform traffic  
Saturated sources  
16 nodes

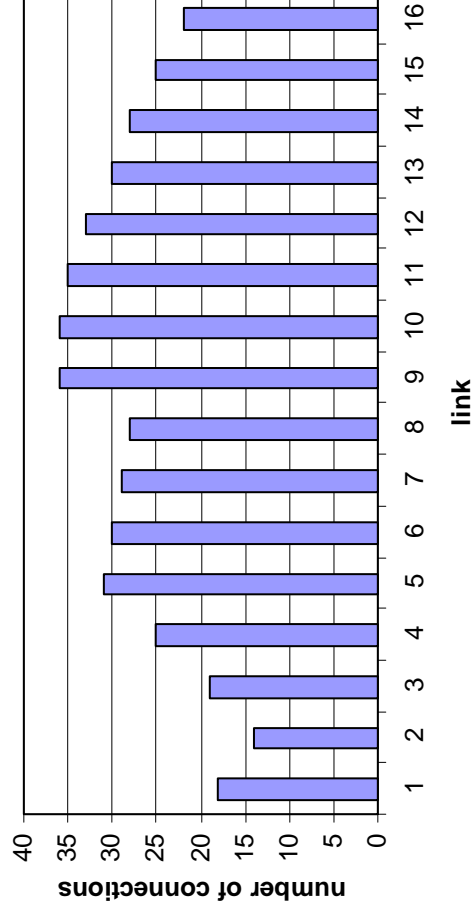


# Number of Connections per Bottleneck Link

## Scenario 2



## Ring 0

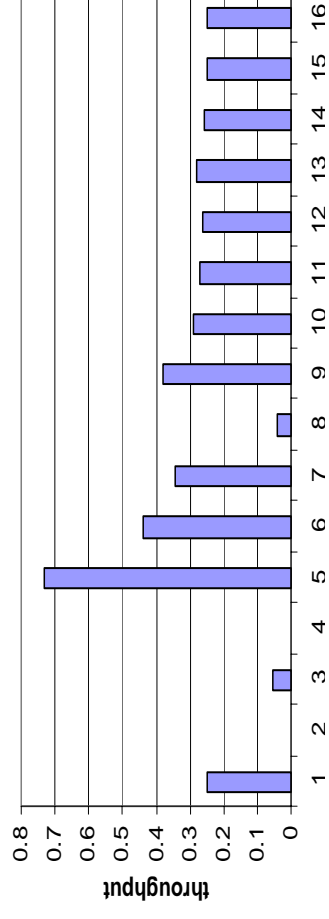


## Ring 1

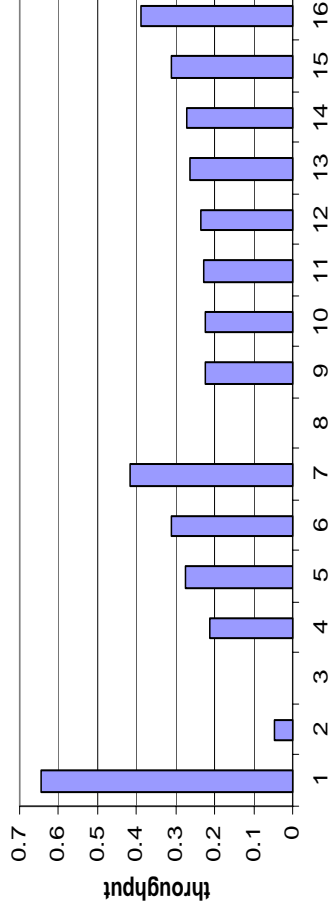
# Throughput per Node

## Scenario 2

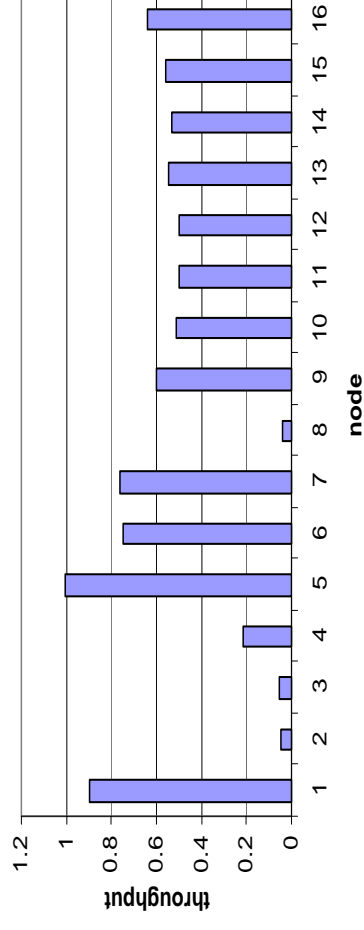
### Ring 0



### Ring 1

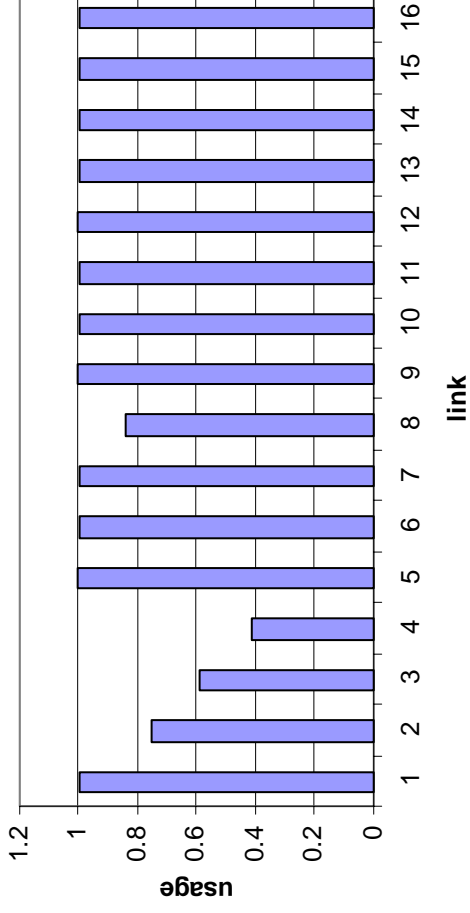


### Ring 0 + Ring 1

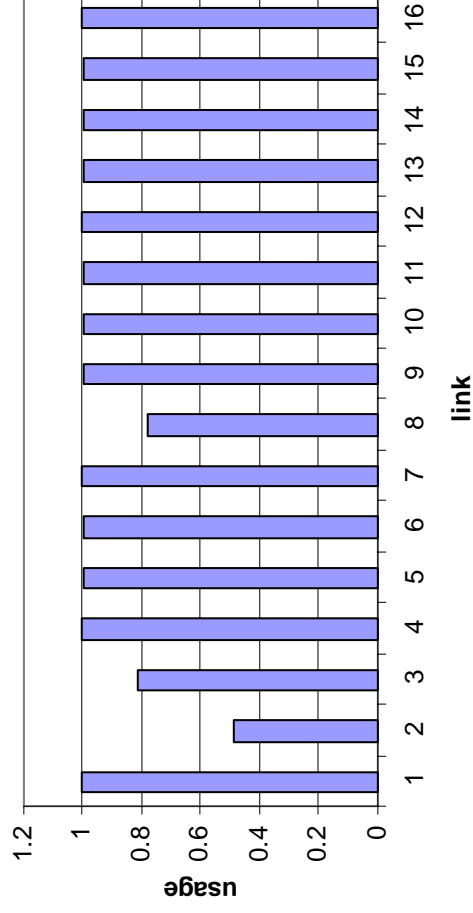


# Link Usage

## Scenario 2



## Ring 0



## Ring 1