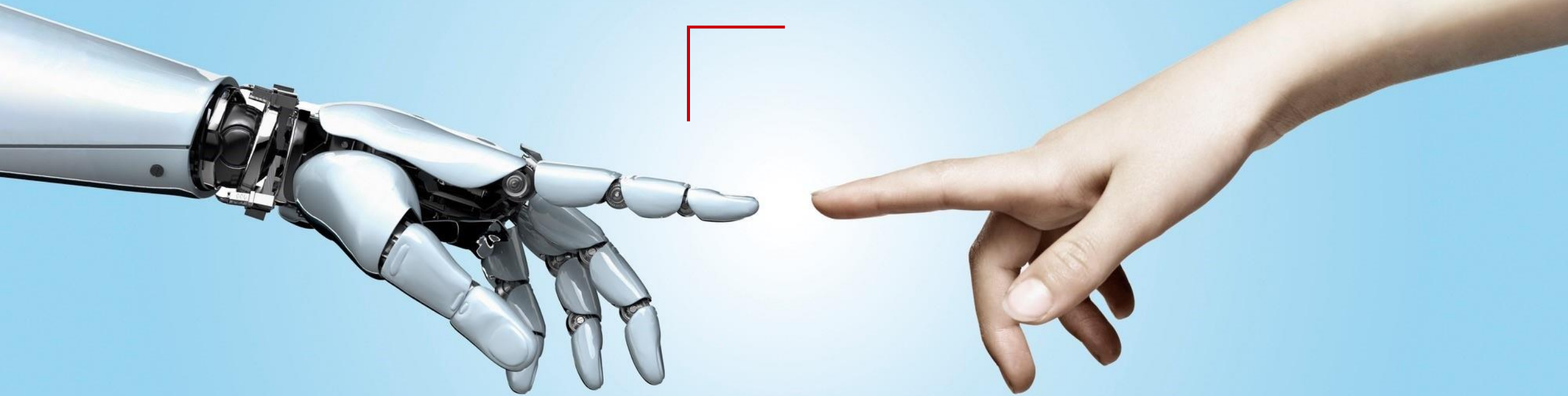


FEC Performance for 200 Gb/s per Lane Optical PHY and Interoperating



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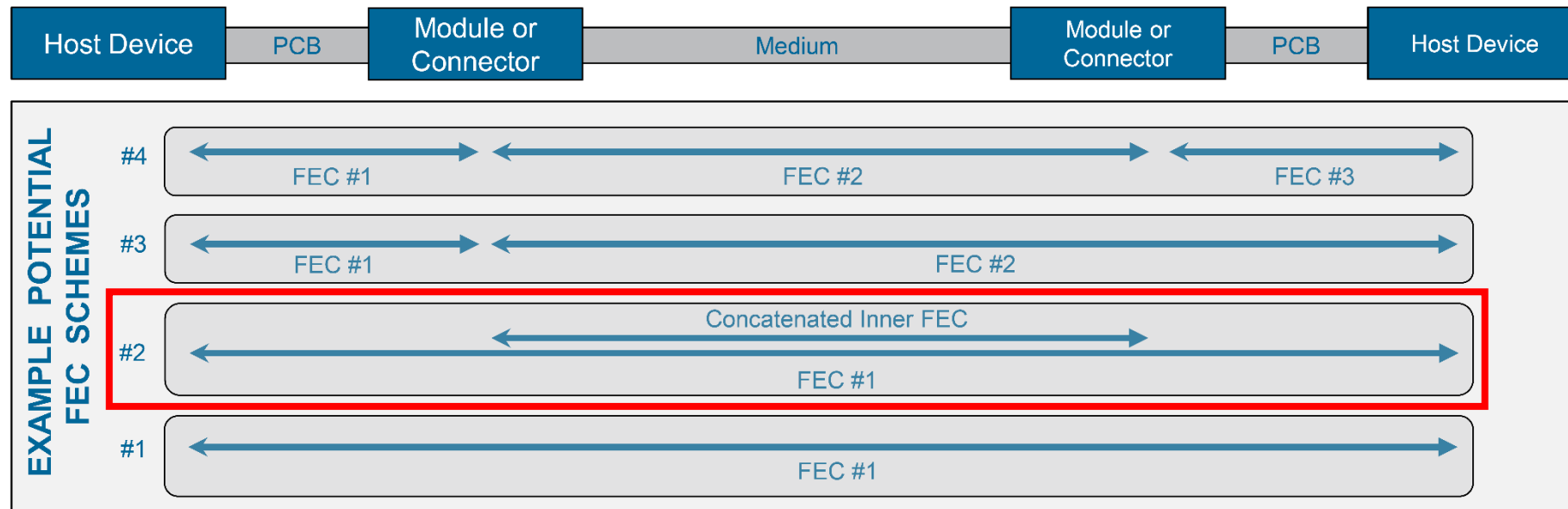


Introduction: 200 Gb/s per Lane PHY

- Various objectives based on 200 Gb/s per lane technology have been adopted in P802.3df/dj for 800G/1.6TbE, including C2C/C2M AUIs, CR/KR electrical PMDs, IM-DD(PAM4) optical PMDs, and potential coherent (16QAM) PMDs.
- In [wang_3df_01b_220928](#), FEC performance for 200 Gb/s per lane electrical PHYs was analyzed based on single-part link model with RS(544,514).
 - 4X codeword interleave has slightly worse FEC performance than 2X in some scenarios, due to the additional FLR penalty.
 - No significant FEC performance difference between 2:1 bit and symbol multiplexing at worst case.

Motivation

- To investigate FEC performance for 200 Gb/s per lane based **multi-part** link model, such as DR/FR PMDs.
 - Multi-part link: multiple analyzed instances (AUIs and optical PHY) between interoperating host devices.
 - Focusing on concatenated scheme: soft-decision BCH inner code protects optical PHY only.

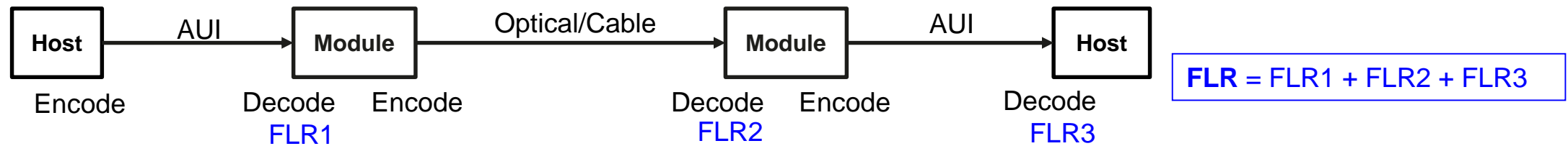


https://www.ieee802.org/3/B400G/public/21_1028/B400G_overview_c_211028.pdf

FLR Evaluation for Different FEC Schemes

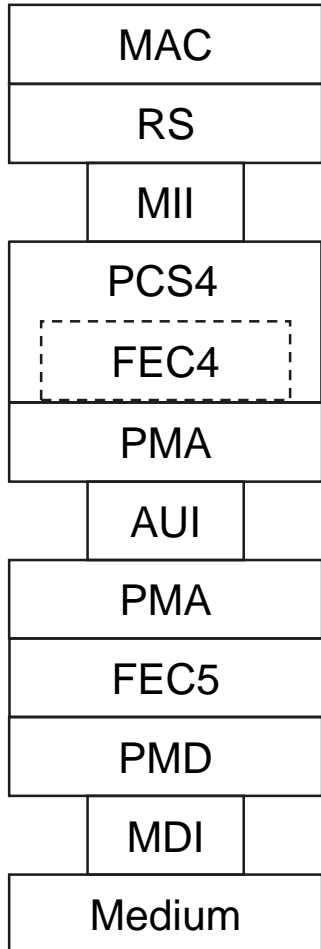
- End-to-end FEC requires both AUI and optical PMD to be within the spec as defined in 802.3bs.
 - AUI BER shall be capped at 1E-5 for each segment.
 - Optical PMD pre-FEC BER target is 2.4E-4 (random error).

- Segmented FEC with RS(544,514) for each segment could result an elevated FLR



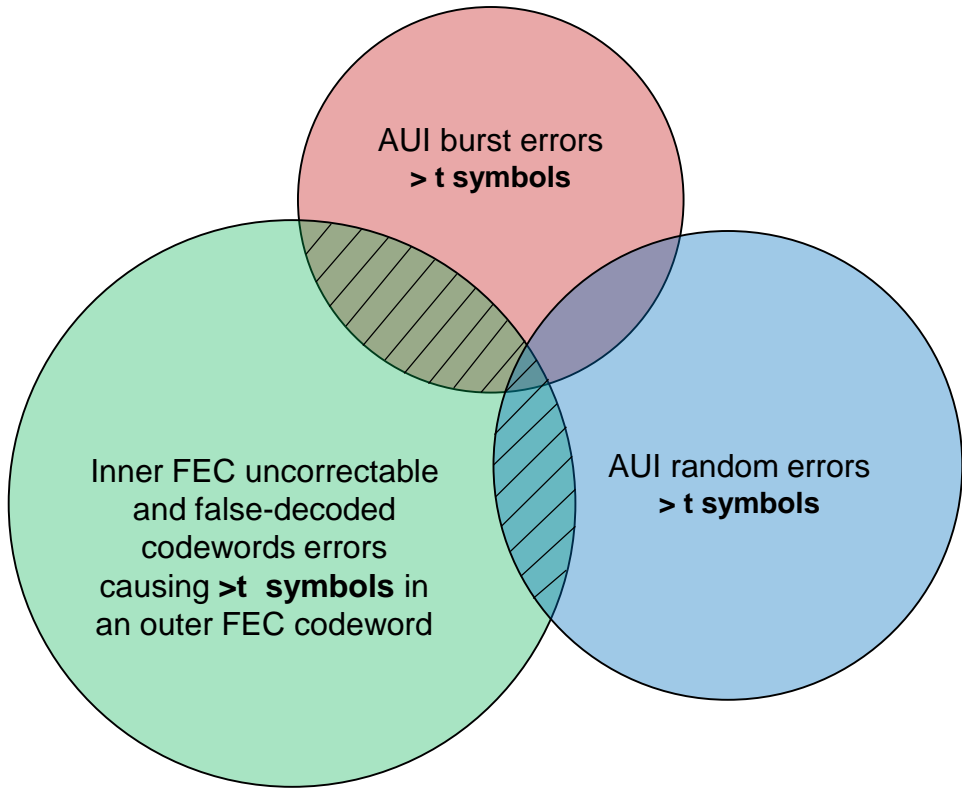
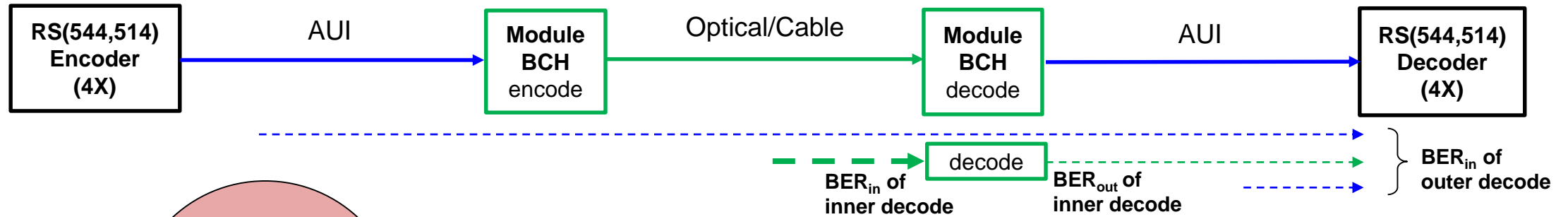
- FEC error marking is required at each decode step for each FEC segment due to re-encode of data ([he b400g_01_210426](#), page 16).
 - Considering 3 FEC segments, the final FLR could be at least 3x as specified in the objective if keeping post-FEC BER@1E-13.
- Concatenated FEC on multi-part link allows higher optical PMD without increasing FLR.
 - Error marking is only performed once in the host device when RS(544,514) is decoded ([he b400g_01_210426](#), page 16).
 - If AUI BER is kept at 1E-5, the pre-FEC BER for optical PMD can be ~ 3E-3.
 - If pre-FEC BER for optical PMD is 2.4E-3, 5E-5 AUI BER (each AUI segment) can be tolerated.

Assumptions for Multi-Part Link FEC Performance



- FEC Scheme: Concatenated.
- Outer code: RS(544,514)
 - 4 codewords interleave
 - Both 802.3df D1.0 PCS (32 lanes) and 4-way RS interleave (8 lanes) are considered.
 - Bit or symbol multiplexing in PMA to form 200 Gb/s per physical lane from 2 PMA lanes.
- Inner code:
 - BCH(144,136), soft-decision decode as in page 6-7 of [he 3df 01a 220308](#).
- AUIs: burst error model with 1-tap DFE introduced error propagation.
 - $a = 0.5, 0.6$ and 0.75 are analyzed as they are the worst cases.
 - Precoding on for $a \geq 0.6$.
- Optical PHY: Random error model, same as 50 and 100 Gb/s per lane in 200/400GbE.

Mathematical Calculation for FEC Performance in Multi-Part Link



*Figure for illustration only, not to show the actual ratio.

- AUI burst + random errors induced uncorrectable RS codeword ratio has been studied in 802.3bs.
 - [anslow_3bs_03_0915](#), [wang_t_3bs_01_0514](#), etc.
- Error distribution in the output of inner code is not random, but appears to be clusters of errors in uncorrectable and false-decoded codewords.
 - [bliss_3df_01a_220517](#), [he_3df_01a_220308](#).
 - When soft-decision decoding is used, it is difficult to quantify the error distribution in RS codewords.
- New method shall be developed to evaluate the outer RS code uncorrectable codeword ratio (UCR).
 - Statistics of minimum independent data groups comprised of inner codeword errors and AUI errors can be used to evaluate the UCR for the outer RS FEC.

Theoretical Analysis of Concatenated Code Performance (Green circle in page 6)

Assumptions: Outer code: 4-way interleaved RS(544,514); Inner code: BCH(144,136).

- Separate the $4 \times \text{RS}(544,514)$ codewords to 32 groups of $5 \times \text{BCH}(144,136)$ codewords.
 - Each group of 5x inner BCH codewords consists of 68×10 -bits RS symbols.
 - Errors in each group of BCH codewords are independent from other groups.
 - Errors in each group are not random because of the non-Gaussian error distribution of BCH decoder output.
- Use $P(E_i)$ as the probability of a group of $5 \times \text{BCH}$ codewords containing E_i number of errors. We can express the uncorrectable codeword ratio (UCR) of the outer RS code as below:

$$\text{UCR caused by inner BCH} = \sum_{\substack{0 \leq E_i \leq 68 \\ 15 < \sum_{i=1}^{32} E_i \leq 544}} \prod_{i=1}^{32} P(E_i) \quad \text{where } 0 \leq E_i \leq 68$$

- $P(E_i)$ can be obtained by simulation on a large number ($>1\text{E}+9$) of BCH codewords in a short period of time.

Theoretical Analysis of Concatenated Code Performance (Including AUI Burst Errors)

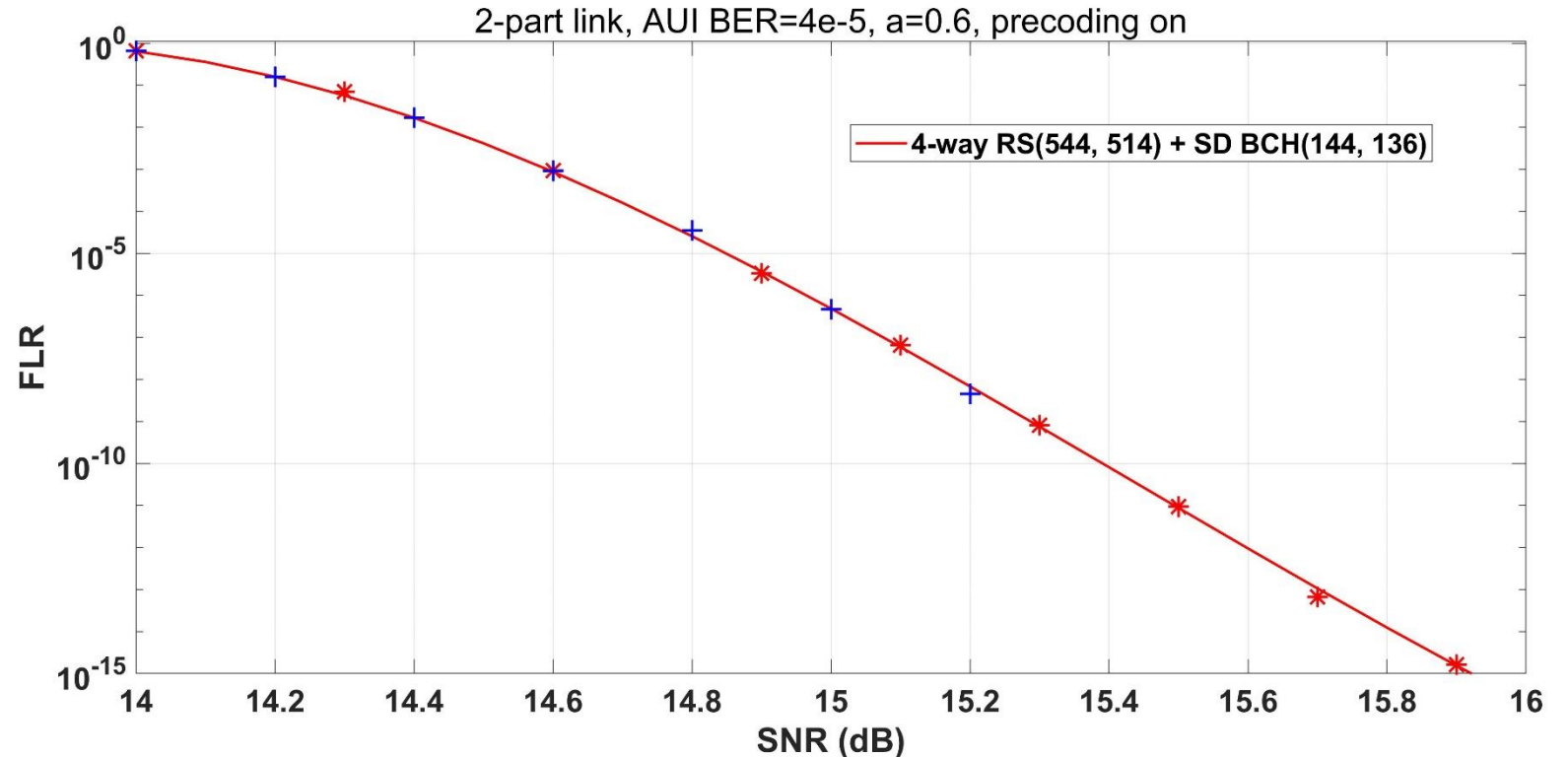
- When burst errors on AUIs are included, the previous model can be extended to larger blocks based on the interleaving scheme.
 - Assuming $4 \times \text{RS}(544,514)$ codewords interleaved to $4 \times n$ lanes (32 or 8).
 - Assuming inner BCH encode is performed on 200G/lane data streams.
 - The minimum independent data group would be based on the 4 inner codeword streams (800GbE).
 - Errors in each group are not random because of the non-Gaussian error distribution of BCH decoder output **AND** AUI bursts.
 - Errors in each group are independent from other groups.
 - The formula can be re-written as below:

$$\text{UCR} = \sum_{\substack{0 \leq E_i \leq 136 \\ 15 < \sum_{i=1}^4 E_i \leq 544}} \prod_{i=1}^4 P(E_i) \quad \text{where } 0 \leq E_i \leq 136$$

- $P(E_i)$ can then be obtained by simulation on a large number of independent data groups.

Verification of Theoretical Analysis

- Monte Carlo simulation results show excellent match to the calculated results.
- Time required to evaluate concatenated code with burst errors on AUI can be significantly reduced.



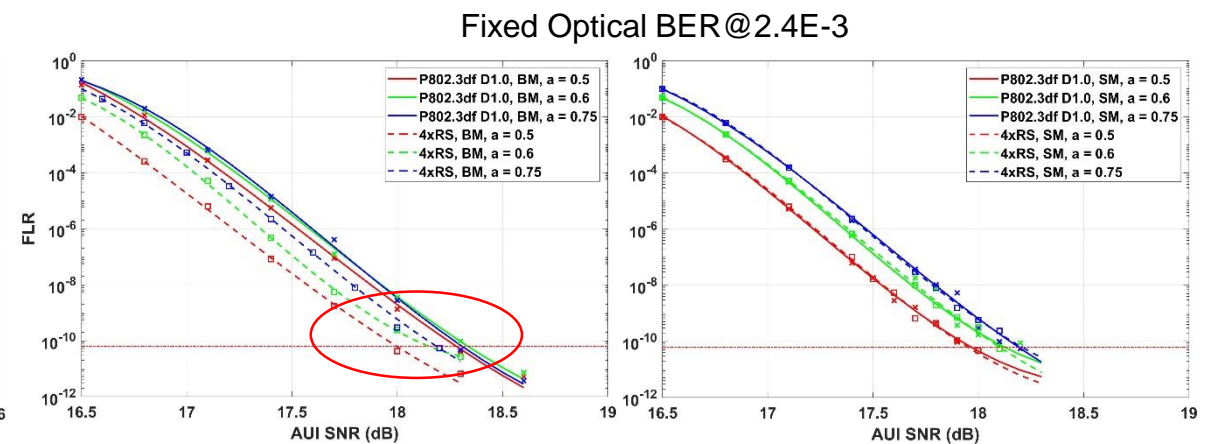
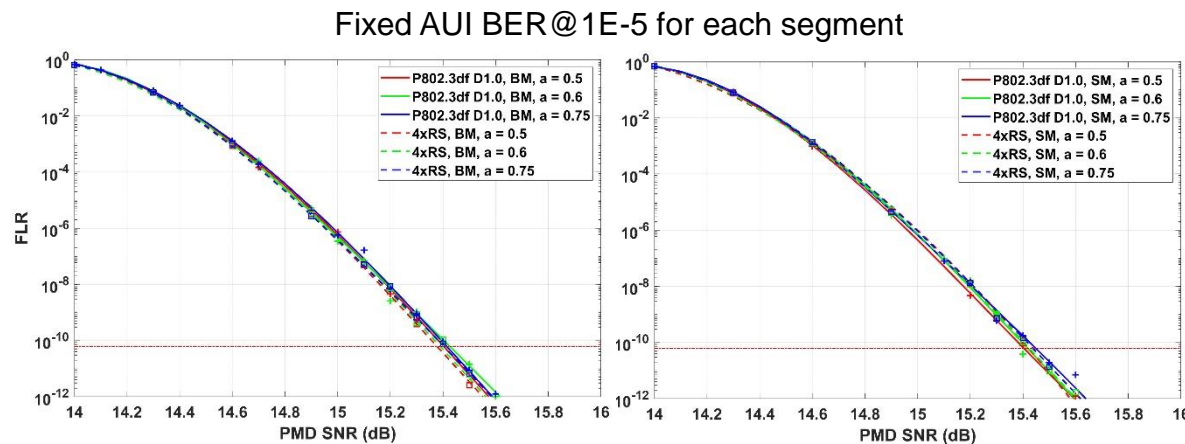
- * Calculated based on model in previous pages.
- + Monte Carlo simulation based on the overall concatenated code.

Concatenated Code Performance: P802.3df PCS vs 4xRS Interleave

- Simulation PCS/PMA setup:

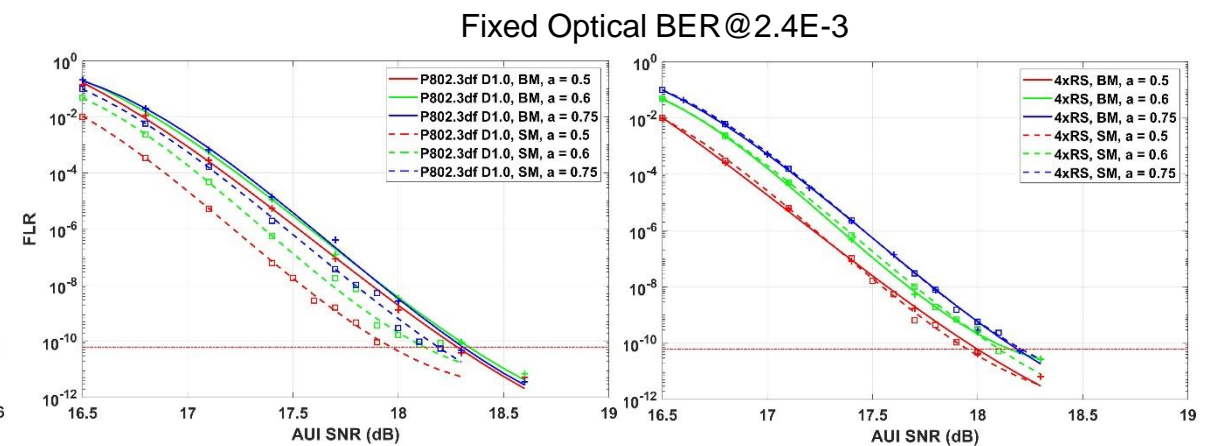
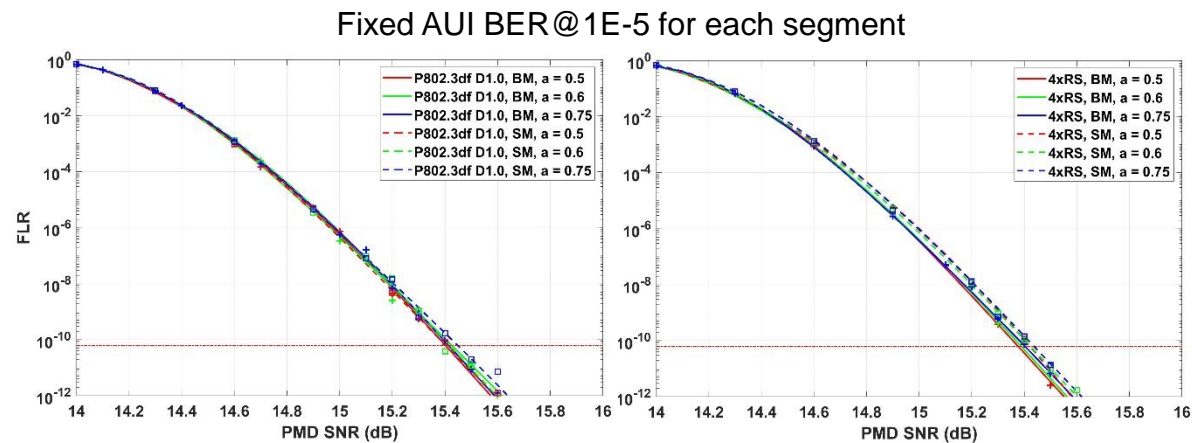
	# of PCS Lanes	PCS to PMA lane muxing	100G/lane to 200G/lane muxing
P802.3df D1.0 BM	32	32:8 bit mux	8:4 bit mux
P802.3df D1.0 SM	32	32:8 symbol mux	8:4 symbol mux
4xRS BM	8	8:8 symbol streams	8:4 bit mux
4xRS SM	8	8:8 symbol streams	8:4 symbol mux

- Two sets of comparisons were performed.
 - Sweeping the optical PMD SNR (random errors), with fixed AUI BER with different burst levels;
 - Sweeping the AUI SNR with different burst levels, with fixed optical PMD SNR/BER (random errors).
- 4x RS interleaving with 8 lanes has better performance in terms of AUI burst tolerance in the right two figures.



Concatenated Code Performance: Bit Mux vs Symbol Mux

- To compare the performance between bit mux and symbol mux for each PCS/PMA setup, the same sets of data were plotted differently.
- 4 RS codewords interleaving could well cover $4E-5$ total AUI BER with bursts.
 - Not much difference can be seen between bit mux and symbol mux if total AUI BER is fixed at $4E-5$.
- Using 8 PCS lanes could allow more errors on the AUI.
 - Symbol mux could help for 32 PCS lanes muxing to 8 PMA lanes.
 - There is no clear advantage for symbol mux if 8 PCS lane is used and the muxing ratio is 2:1.



FEC Performance Results to Meet BER/FLR Objective

- The required SNR and DER at the slicer input, and the corresponding BER values at input of FEC decode to meet FLRs equivalent (6.2E-11) to that of a BER of 1E-13 are:

	AUI (Fixed total BER)			Optical PMD			AUI (Total BER)			Optical PMD (Fixed SNR)		
	SNR	DER	BER*	SNR	DER	BER	SNR	DER	BER*	SNR	DER	BER
a	P802.3df D1.0, 32:8 bit mux + 8:4 bit mux						P802.3df D1.0, 32:8 bit mux + 8:4 bit mux					
0.5	19.12	4.0E-5	4.0E-5	15.405	6.31E-03	3.16E-03	18.28	1.83E-04	1.83E-04	15.70	4.8E-3	2.4E-3
0.6**				15.425	6.20E-03	3.10E-03	18.34	1.65E-04	1.65E-04			
0.75**				15.415	6.26E-03	3.13E-03	18.31	1.74E-04	1.74E-04			
a	P802.3df D1.0, 32:8 symbol mux + 8:4 symbol mux						P802.3df D1.0, 32:8 symbol mux + 8:4 symbol mux					
0.5	19.12	4.0E-5	4.0E-5	15.405	6.31E-03	3.16E-03	17.97	3.00E-04	3.00E-04	15.70	4.8E-3	2.4E-3
0.6**				15.42	6.23E-03	3.12E-03	18.12	2.37E-04	2.37E-04			
0.75**				15.45	6.06E-03	3.03E-03	18.19	2.12E-04	2.12E-04			
a	4xRS, 8:8 + 8:4 bit mux						4xRS, 8:8 + 8:4 bit mux					
0.5	19.12	4.0E-5	4.0E-5	15.38	6.45E-03	3.23E-03	18.00	2.86E-04	2.86E-04	15.70	4.8E-3	2.4E-3
0.6**				15.39	6.40E-03	3.20E-03	18.15	2.26E-04	2.26E-04			
0.75**				15.405	6.31E-03	3.16E-03	18.19	2.12E-04	2.12E-04			
a	4xRS, 8:8 + 8:4 symbol mux						4xRS, 8:8 + 8:4 symbol mux					
0.5	19.12	4.0E-5	4.0E-5	15.420	6.23E-03	3.12E-03	17.95	3.09E-04	3.09E-04	15.70	4.8E-3	2.4E-3
0.6**				15.425	6.20E-03	3.10E-03	18.10	2.45E-04	2.45E-04			
0.75**				15.44	6.12E-03	3.06E-03	18.20	2.08E-04	2.08E-04			

* These values are the BER including the additional errors due to the bursts and effect of precoding. The values have been multiplied by 2.

** Precoding is turned on for a = 0.6 and 0.75.

Summary

- Mathematical model to evaluate the performance of concatenated code is introduced.
- The PCS/PMA multiplexing scheme will influence the concatenated FEC capability for multi-part link with burst errors.
 - $4\times$ codewords interleave can provide excellent burst tolerance for AUI.
 - Symbol mux outperforms bit mux if there are 32 PCS lanes.
 - No significant FEC performance difference between 2:1 bit and symbol multiplexing for 800 GbE with 8 PCS lanes and 1.6 TbE with 16 PCS lanes.
 - More work is underway for 200G/lane AUIs.

Acknowledgement

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 - Nianqi Tang, Huawei Technologies

Thank You!