

# **MLSE Sequence Truncation Implementation Penalty**

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# Motivation

- MLSE implementation penalty is still TBD in Draft 1.1 ( $Q$  in Equation 178A-36)
- It is one of the open “Big Ticket Items” after comment resolutions in June Electronic Interim ([lusted\\_3dj\\_elec\\_01\\_240620.pdf](#))
- In [shakiba\\_3dj\\_01a\\_2403.pdf](#) the following implementation issues were listed and analyzed:
  - ❖ Pre-screening
  - ❖ Sequence Truncation
  - ❖  $\alpha$  Mismatch
  - ❖ Quantization Noise
- This contribution highlights sequence truncation as the primary implementation constraint specific to MLSE and proposes an analytic approach to quantify it
- Presented data is based on COM version “com\_ieee8023\_93a\_460beta3\_**hs1p0**”
  - ❖ Customization is to include implementation penalty due to truncation

# Introduction

- Pre-screening provides a means of removing the MLSE  $\Delta COM$  improvement if the pre-MLSE signal quality is not suitable for clock recovery
  - ❖ It's been implemented in the COM code by ignoring MLSE and setting  $\Delta COM = 0$  if  $DER$  before MLSE is higher than a set threshold (defaulted to 1E-2)
- Contributions [shakiba\\_3dj\\_01a\\_2403.pdf](#) and [shakiba\\_3dj\\_02\\_2405.pdf](#) demonstrated that quantization noise impact goes well beyond MLSE and suggested a direct method to include it as a new noise component at the COM and system modeling levels
- Contribution [healey\\_3dj\\_01b\\_2405.pdf](#) also recognized the importance of quantization noise and discussed the above and another approach to account for it
  - ❖ This contribution appears to favour the other approach that uses  $\eta_0$  as a knob to mimic the effect
- Currently,  $\alpha$  mismatch is not recognized as a critical concern

# Sequence Truncation

- One of the practical simplifications to MLSE is to limit length of the sequence
- There are several ways this can be implemented, but they all share a similar concept
- The case considered here for analysis is the case where the sequence processing and trace-back are both limited to a truncated length
- As a result:
  - 1) Error events shorter than *trunc* will still be entirely processed and Equation U1.c directly applies
    - ❖ Equation U1.c executes to its first *trunc* – 1 terms
  - 2) Longer error events will be partially processed and in Equation U1.c:
    - ❖ The MLSE sequence noise will have *trunc* terms
    - ❖ The PDF convolution expression iterates *trunc* – 1 times
    - ❖ The correlation matrix  $\rho_{noise,jEE}$  truncates to a  $\rho_{noise,truncEE}$  (*trunc* × *trunc*) sub-matrix

# Sequence Truncation in Equation U1.c\*

$$PDF_{noise,jEE}(x) = \begin{cases} PDF_{noise}(x) * \text{conv}_{i=2}^j \frac{1}{1-\alpha} PDF_{noise}\left(\frac{x}{1-\alpha}\right) * \frac{1}{\alpha} PDF_{noise}\left(\frac{x}{\alpha}\right) & , j < trunc \\ PDF_{noise,truncEE}(x) = PDF_{noise}(x) * \text{conv}_{i=2}^{trunc} \frac{1}{1-\alpha} PDF_{noise}\left(\frac{x}{1-\alpha}\right) & j \geq trunc \end{cases}$$

$$\rho_{noise,jEE} = \begin{cases} \rho_{noise,jEE}((j+1) \times (j+1)) & , j < trunc \\ \rho_{noise,truncEE} = \rho_{noise,jEE}((1:trunc) \times (1:trunc)) & j \geq trunc \end{cases}$$

$$DER_{MLSE,trunc} \approx \sum_{j=1}^{trunc-1} \left(\frac{L-1}{L}\right)^{j-1} \left( CDF_{noise,jEE} \left( -A_s \frac{(\text{trace}(\rho_{noise,jEE}))^{\frac{3}{2}}}{\sqrt{\Sigma_{vertical} \Sigma_{horizontal}(\rho_{noise,jEE})}} \right) \right) + L \left(\frac{L-1}{L}\right)^{trunc-1} \left( CDF_{noise,truncEE} \left( -A_s \frac{(\text{trace}(\rho_{noise,truncEE}))^{\frac{3}{2}}}{\sqrt{\Sigma_{vertical} \Sigma_{horizontal}(\rho_{noise,truncEE})}} \right) \right)$$

\* Rewritten format based on the Draft 1.0 comments (Annex 178A)

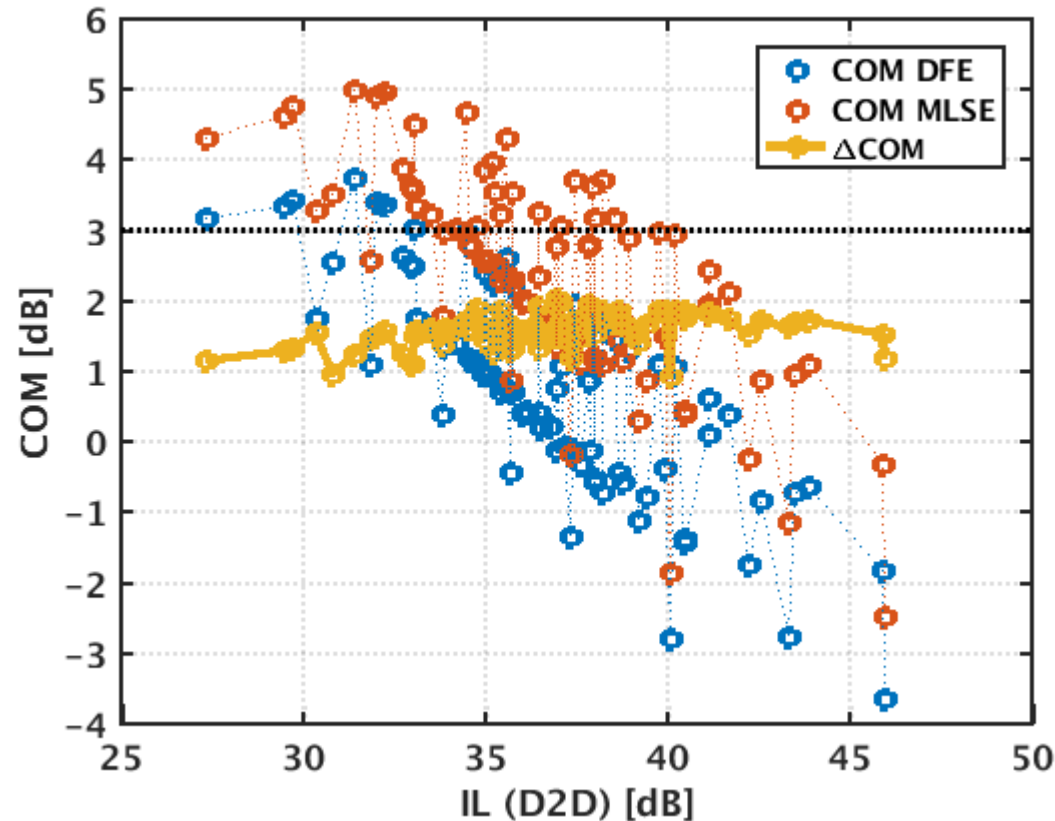
- This leads to a sequence truncation penalty of:

$$Q_{trunc} \approx 20 \log_{10} \left( \frac{CDF_{noise}^{-1}(DER_{MLSE})}{CDF_{noise}^{-1}(DER_{MLSE,trunc})} \right)$$

- Which is basically the reduction in SNR due to truncation

# Test Results\* – Without Truncation

- With the latest COM version (mostly MMSE RxFFE changes and MLSE updates), for the test cases equation U1.c results in an MLSE  $\Delta COM$  with Min = 0.93dB, Max = 2.04dB, and Ave = 1.56dB (still no MLSE implementation penalty,  $Q = 0$ )

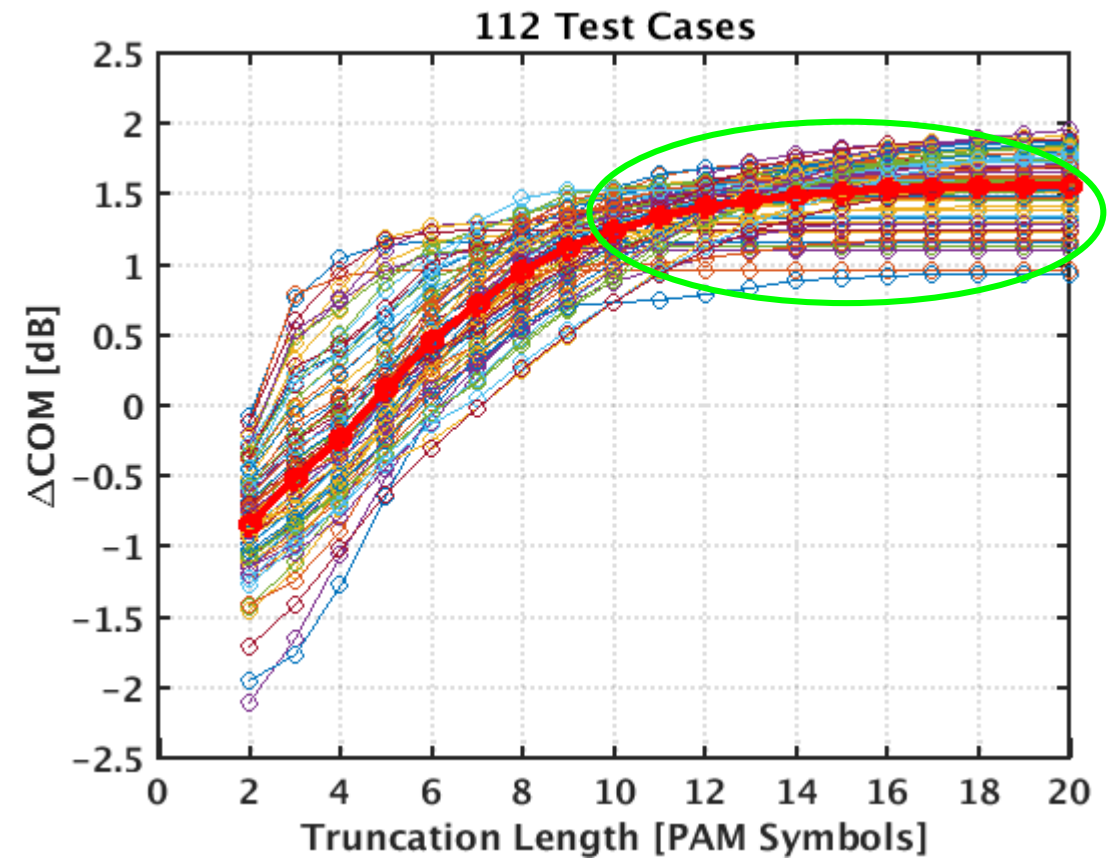


\* For the test channels see the Appendix

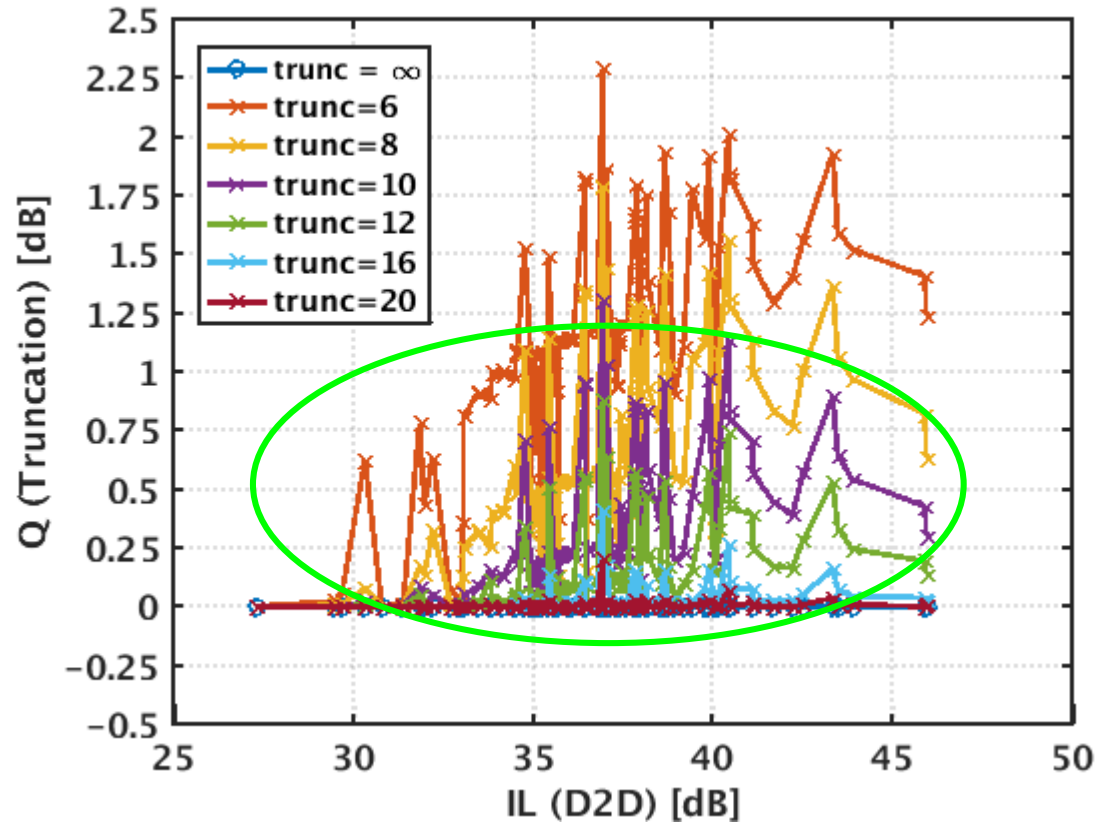
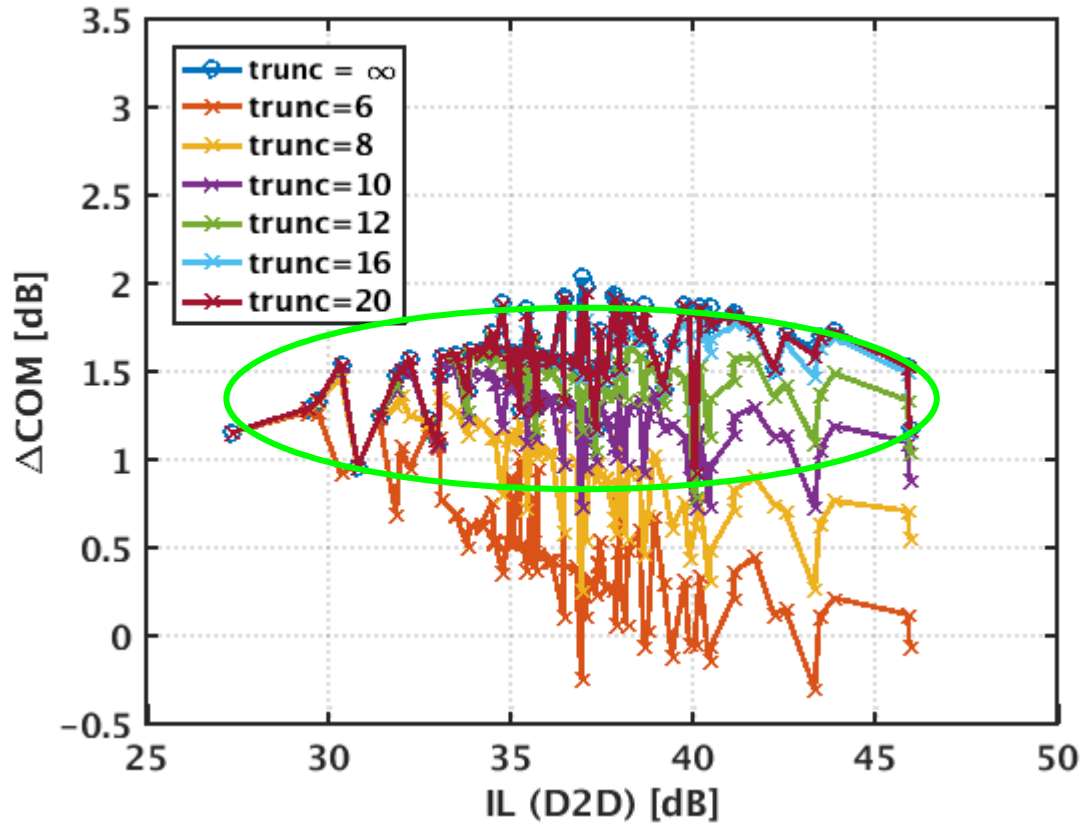


# Test Results – With Truncation, Overall Picture

- There is a trade off between performance vs. complexity and latency (reasons for truncation)
- Data supports why implementations have usually chosen truncating to no less than 10
- Some implementations have chosen around 20
- Truncating in the range of 10-20 seems to be a reasonable choice
- For our purpose, with some pessimism, the lower end of the range (~ 10-15) may be considered

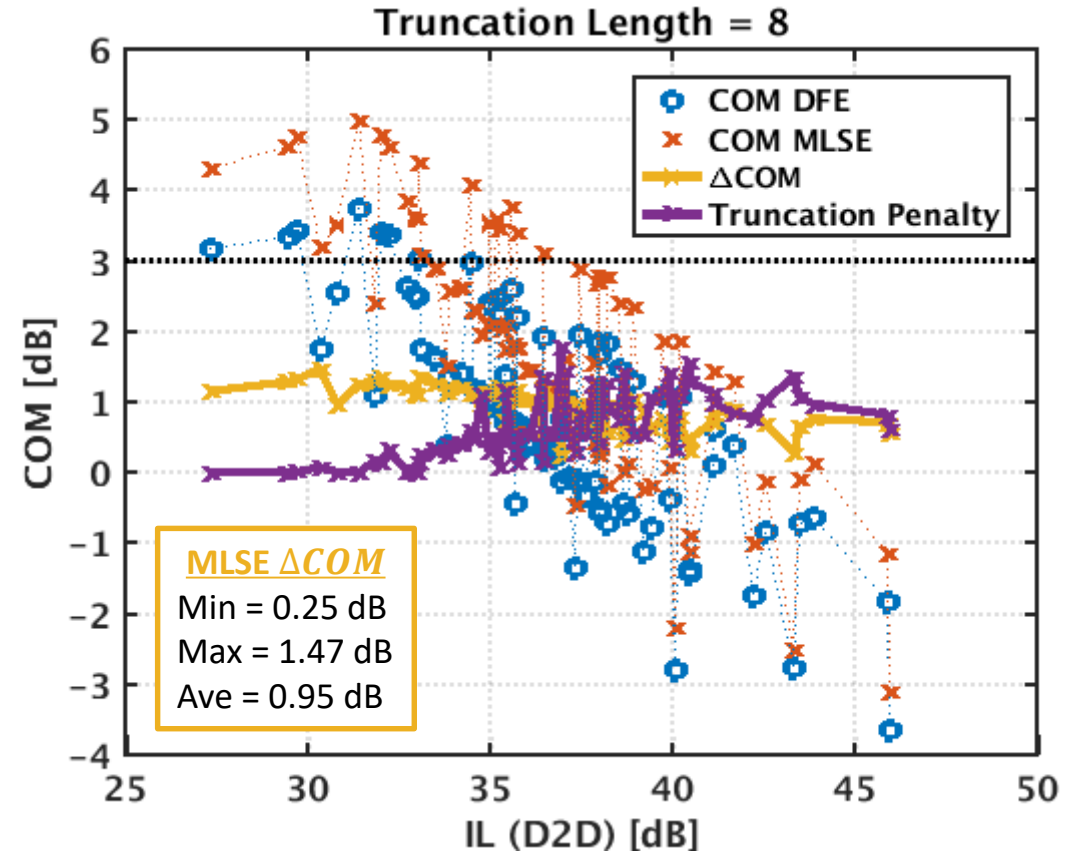
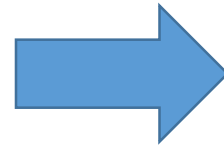
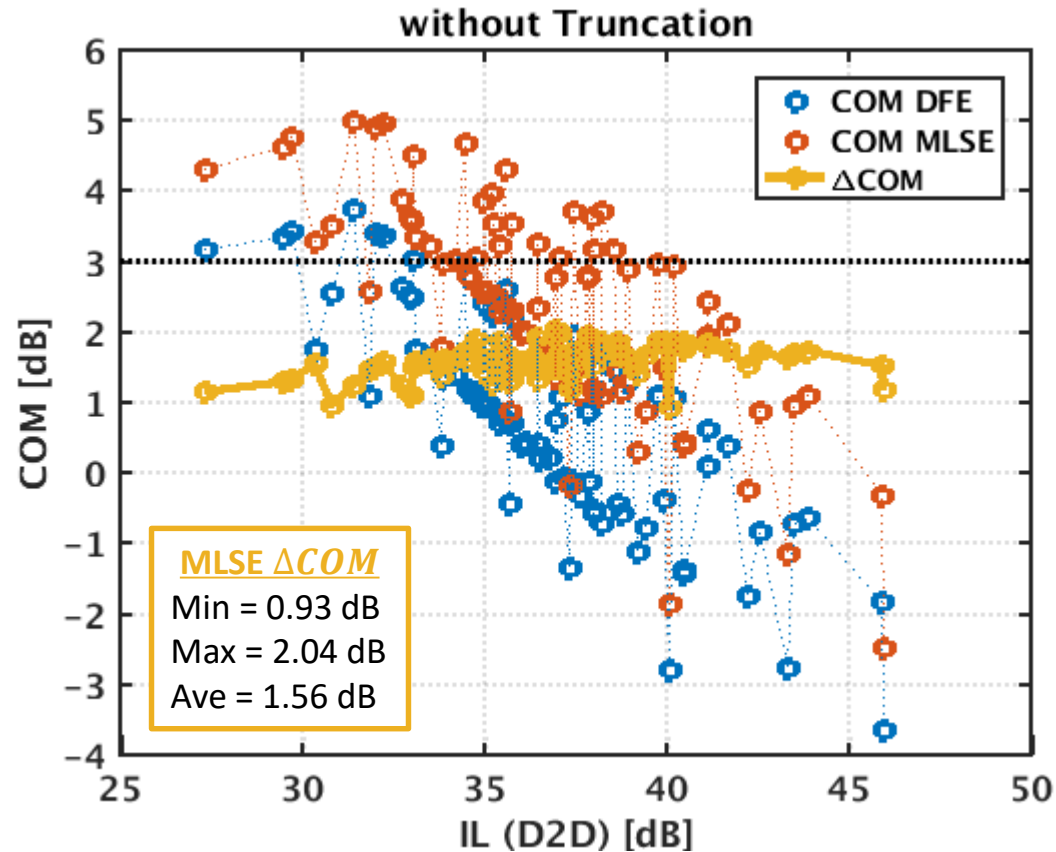


# Test Results – With Truncation, Versus IL



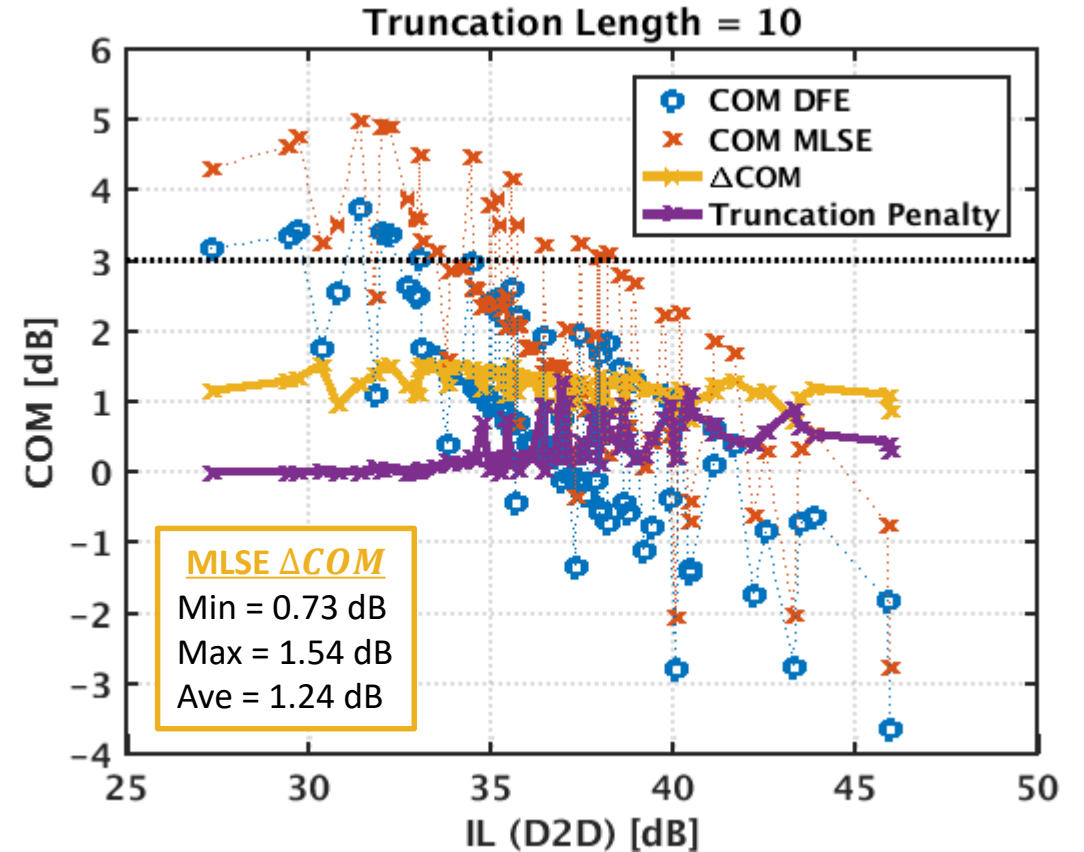
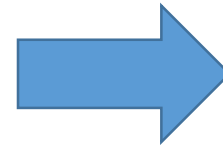
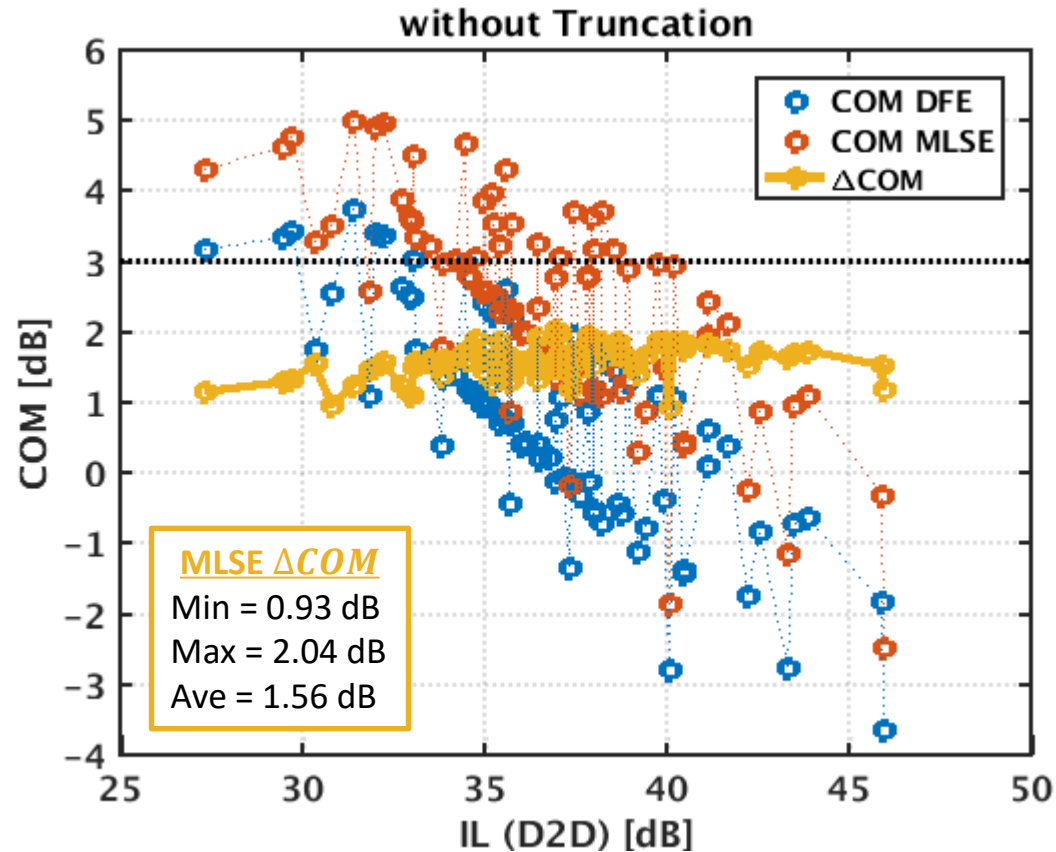
- Generally speaking, truncation penalty increases with insertion loss
- The slight drops at the high loss end are from cases that most likely fail anyway
- This is a trend that many people may expect and may like 😊

# Test Results – With Truncation, $trunc = 8$



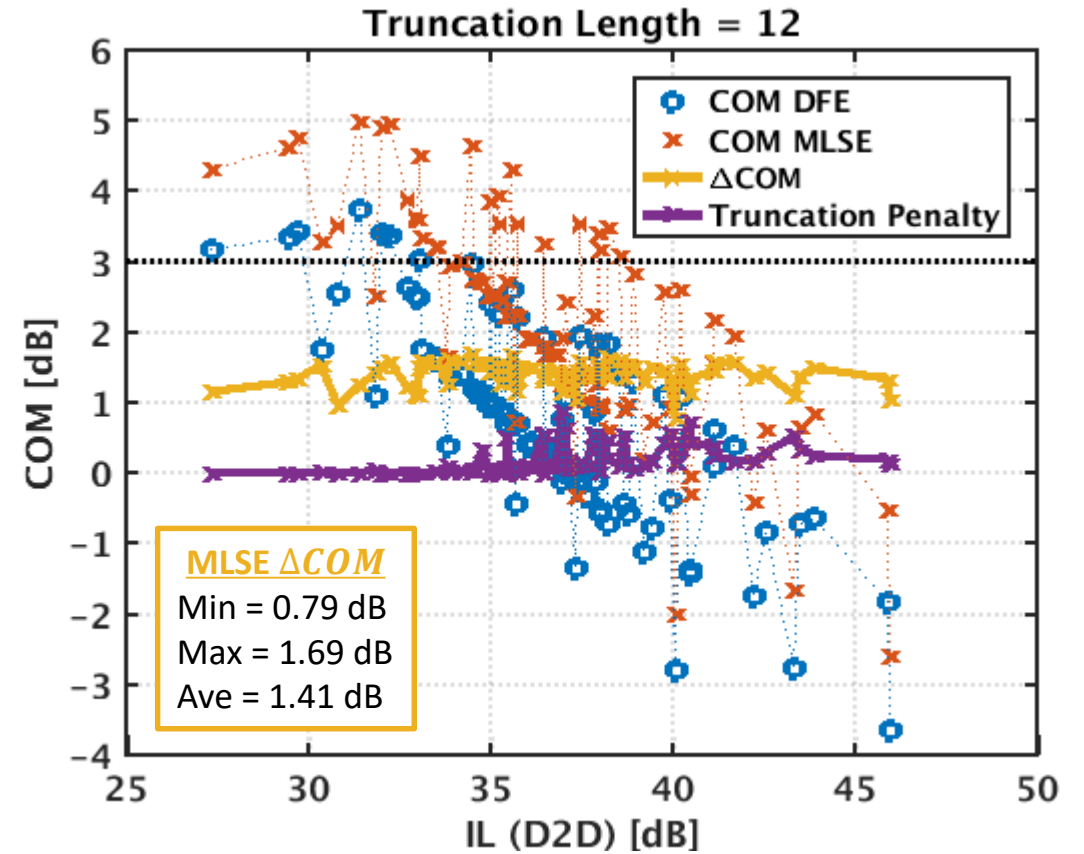
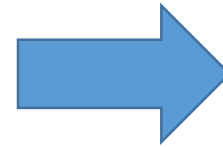
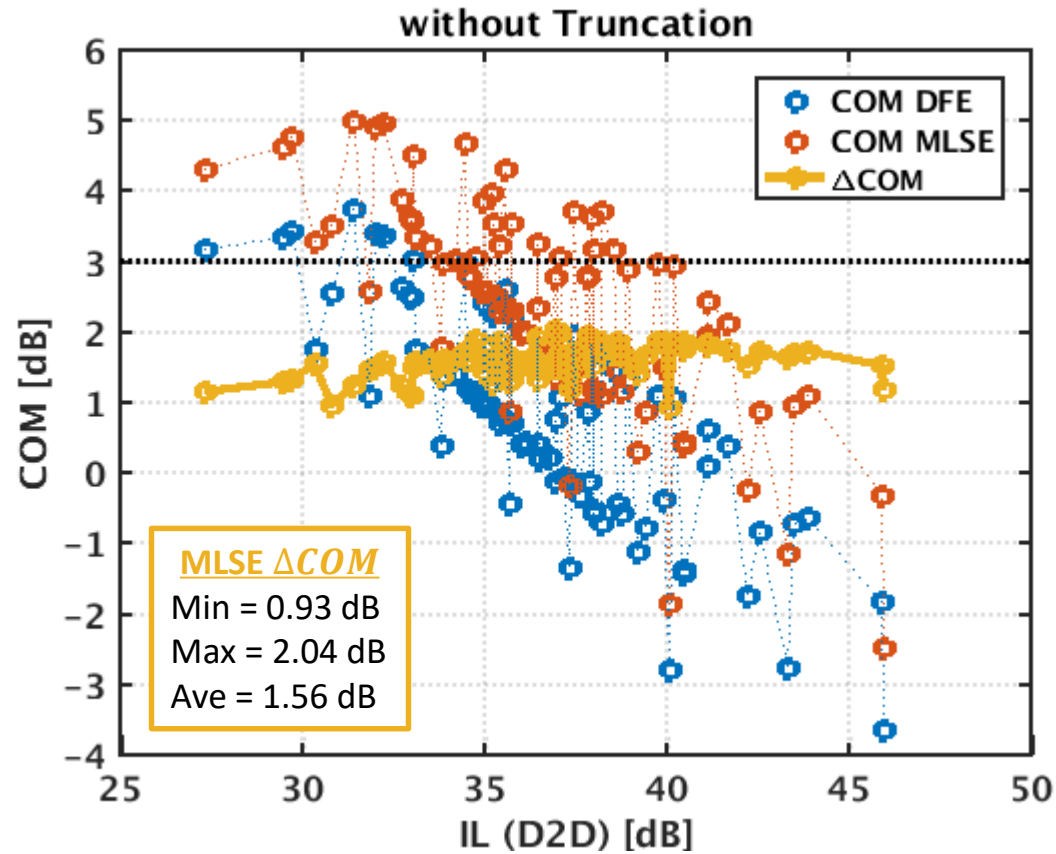
- A truncation length of 8 penalizes MLSE by an average of 0.61dB
- The resulting  $\Delta$ COM averages to 0.95dB, concentrated around 30-40dB IL, which is a critical range where MLSE has the most impact

# Test Results – With Truncation, $trunc = 10$



- A truncation length of 10 penalizes MLSE by an average of 0.32dB
- The resulting  $\Delta$ COM averages to 1.24dB, concentrated around 30-40dB IL, which is a critical range where MLSE has the most impact

# Test Results – With Truncation, $trunc = 12$



- A truncation length of 12 penalizes MLSE by an average of 0.16dB
- The resulting  $\Delta$ COM averages to 1.41dB, concentrated around 30-40dB IL, which is a critical range where MLSE has the most impact

# Options

- The following options have been discussed for including the MLSE implementation penalty ( $Q$  in equation 178A-36):
  - 1) Subtract an agreed upon fix amount ( $Q_{cte}$ ) from  $\Delta COM$  ( $Q = Q_{cte}$ )
    - ☹️ Difficult to justify and partially defeating the prospect of calculating  $\Delta COM$  using U1.c on a case basis
  - 2) Limit  $\Delta COM$  to an agreed upon maximum value ( $\Delta COM_{max}$ )  
$$Q = \begin{cases} 0 & , \Delta COM \leq \Delta COM_{max} \\ \Delta COM - \Delta COM_{max} & , \Delta COM > \Delta COM_{max} \end{cases}$$
    - ☹️ Difficult to justify and partially defeating the prospect of calculating  $\Delta COM$  using U1.c on a case basis
  - 3) Derate  $\Delta COM$  by an agreed upon factor ( $Q \propto \Delta COM$ )
    - ☹️ Difficult to justify and partially defeating the prospect of using U1.c to calculate  $\Delta COM$
  - 4) Use the proposed method in this contribution and use the truncation SNR penalty ( $Q_{trunc}$  in slide 7) as  $Q$  with an agreed upon value for  $trunc$ 
    - 😊 Same justification and inline with the prospect and methodology of calculating  $\Delta COM$  using U1.c

# Summary and Conclusion

- MLSE implementation penalty is still TBD ( $Q$  in Equation 178A-36)
- This contribution extended the same analysis approach of calculating MLSE  $\Delta COM$  using U1.c to calculating the MLSE sequence truncation penalty,  $Q_{trunc}$
- With the view of truncation being the primary reason for MLSE implementation constraint,  $Q_{trunc}$  can represent  $Q$  in equation 178A-36
- This option is preferred over the other options of using a constant penalty, limiting  $\Delta COM$  to a maximum value, or derating  $\Delta COM$
- The option is inline with the method and analysis used to calculate MLSE  $\Delta COM$  using U1.c
- Contributions are encouraged to agree upon the method and parameters

# Backup Slides



# Test Channels (KR/CR)

Channel #	Channel Source
1	<a href="https://www.ieee802.org/3/dj/public/tools/CR/lim_3dj_03_230629.zip">https://www.ieee802.org/3/dj/public/tools/CR/lim_3dj_03_230629.zip</a>
2	<a href="https://www.ieee802.org/3/dj/public/tools/CR/lim_3dj_04_230629.zip">https://www.ieee802.org/3/dj/public/tools/CR/lim_3dj_04_230629.zip</a>
3 – 7	<a href="https://www.ieee802.org/3/dj/public/tools/CR/kocsis_3dj_02_2305.zip">https://www.ieee802.org/3/dj/public/tools/CR/kocsis_3dj_02_2305.zip</a>
8 – 34	<a href="https://www.ieee802.org/3/dj/public/tools/KR/mellitz_3dj_02_elec_230504.zip">https://www.ieee802.org/3/dj/public/tools/KR/mellitz_3dj_02_elec_230504.zip</a>
35 – 40	<a href="https://www.ieee802.org/3/dj/public/tools/CR/shanbhag_3dj_01_2305.zip">https://www.ieee802.org/3/dj/public/tools/CR/shanbhag_3dj_01_2305.zip</a>
41 – 44	<a href="https://www.ieee802.org/3/dj/public/tools/KR/shanbhag_3dj_02_2305.zip">https://www.ieee802.org/3/dj/public/tools/KR/shanbhag_3dj_02_2305.zip</a>
45 – 80	<a href="https://www.ieee802.org/3/dj/public/tools/KR/weaver_3dj_02_2305.zip">https://www.ieee802.org/3/dj/public/tools/KR/weaver_3dj_02_2305.zip</a>
81 – 88	<a href="https://www.ieee802.org/3/dj/public/tools/KR/weaver_3dj_elec_01_230622.zip">https://www.ieee802.org/3/dj/public/tools/KR/weaver_3dj_elec_01_230622.zip</a>
89	<a href="https://www.ieee802.org/3/dj/public/tools/CR/lim_3dj_07_2309.zip">https://www.ieee802.org/3/dj/public/tools/CR/lim_3dj_07_2309.zip</a>
90 – 96	<a href="https://www.ieee802.org/3/dj/public/tools/KR/akinwale_3dj_01_2310.zip">https://www.ieee802.org/3/dj/public/tools/KR/akinwale_3dj_01_2310.zip</a>
97 – 100	<a href="https://www.ieee802.org/3/dj/public/tools/CR/akinwale_3dj_02_2311.zip">https://www.ieee802.org/3/dj/public/tools/CR/akinwale_3dj_02_2311.zip</a>
101 – 112	<a href="https://www.ieee802.org/3/dj/public/tools/CR/weaver_3dj_02_2311.zip">https://www.ieee802.org/3/dj/public/tools/CR/weaver_3dj_02_2311.zip</a>

# COM Config

Table 93A-1 parameters				I/O control			Table 93A-3 parameters				SAVE_CONFIG2MAT	0		
Parameter	Setting	Units	Information	DIAGNOSTICS	0	logical	Parameter	Setting	Units	Information	RX_CALIBRATION	Receiver testing		
f_b	106.25	GHz		DISPLAY_WINDOW	0	logical	package_tl_gamma0_a1_a2	[5e-4 0.00065 0.0003]			0	logical		
f_min	0.05	GHz		CSV_REPORT	0	logical	package_tl_tau	0.006141	ns/mm		Sigma_BBN_step	5.00E-03	V	
Delta_f	0.01	GHz		RESULT_DIR	results\C2M_(date)		package_Z_c	02; 70 70; 80 80; 100	Ohm		ICN parameters			
C_d	[0.4e-4 0.9e-4 1.1e-4; 0.4e-4 0.9e-4 1.1e-4]	nF	[TX RX]	SAVE_FIGURES	0	logical	z_p (TX)	*1 1 1 1; 1 1 1 1; 0.5	mm	[test cases to run]	f_v	0.278	Fb	
L_s	[0.13 0.15 0.14; 0.13 0.15 0.14]	nH	[TX RX]	Port Order	[1 3 2 4]		z_p (NEXT)	*1 1 1 1; 1 1 1 1; 0.5	mm	[test cases]	f_f	0.278	Fb	
C_b	[0.3e-4 0.3e-4]	nF	[TX RX]	RUNTAG	C2MTP1a_COM_model		z_p (FEXT)	*1 1 1 1; 1 1 1 1; 0.5	mm	[test cases]	f_n	0.278	Fb	
R_0	5.00E+01	Ohm		COM_CONTRIBUTION	1	logical	z_p (RX)	*1 1 1 1; 1 1 1 1; 0.5	mm	[test cases]	f_2	61.625	GHz	
R_d	[50 50]	Ohm	[TX RX]	TDR and ERL options			C_p	[0.4e-4 0.4e-4]	nF	[test cases]	A_ft	0.450	V	
PKG_NAME	PKG_HR_CLASSB	PKG_Module	TX RX	TDR	1	logical	Operational			A_nt	0.450	V		
A_v	0.413	V		ERL	1	logical	ERL_Pass threshold	10	dB		Parameter Setting			
A_fe	0.413	V		ERL_ONLY	0	ns	COM_Pass threshold	3	db		board_tl_gamma0_a1_a2	[0.644084e-4 3.6036e-05]	1.4 db/in @ 53.125G	
A_ne	0.608	V		TR_TDR	0.01		DER_0	2.50E-05			board_tl_tau	5.790E-03	ns/mm	
z_p select	[4]			N	4000	logical	T_r	4.00E-03	ns		board_Z_c	100	Ohm	
L	4	L		TDR Butterworth	1		FORCE_TR	1	logical		z_bp (TX)	32	mm	
M	32			beta_x	0						z_bp (NEXT)	32	mm	
filter and En				rho_x	0.618		PMD_type	C2C			z_bp (FEXT)	32	mm	
f_r	0.58	*fb		TDR_W_TXPKG	0	UI					z_bp (RX)	32	mm	
c(0)	0.55		min	N_bx	20		T_O	0	mUI		C_0	[0.2e-4 0]	nF	
c(-1)	0		[min:step:max]	fixture delay time	[0 0]		samples_for_C2M	100	samples/UI		C_1	[0.2e-4 0]	nF	
c(-2)	0		[min:step:max]	Tukey_Window	1		EW	0			Include PCB		0	logical
c(-3)	0		[min:step:max]	Noise, jitter			MLSE	3	logical	Selections (rectangle, gaussian, dual, rayleigh, triangle)				
c(-4)	0		[min:step:max]	sigma_RJ	0.01	UI	ts_anchor	1		Histogram_Window_Weight	gaussian	selection		
c(1)	0		[min:step:max]	A_DD	0.02	V^2/GHz	sample_adjustment	[-32 32]		Qr	0.02	UI		
N_b	1	UI		eta_0	1.25E-08	dB	Local Search	0						
b_max(1)	0.85	As/dffe1		SNR_TX	33		Filter: RxFFE							
b_max(2..N_b)	0.3	As/dfe2..N_b		R_LM	0.95		f_fe_pre_tap_len	5	UI					
b_min(1)	0	As/dffe1		DER_COR			1.00E-02		UI					
b_min(2..N_b)	-0.15	S	As/dfe2..N_b	ENOB	32		f_fe_post_tap1_max	1	(normalized)					
g_DC	-1	dB	[min:step:max]	trunc	128		f_fe_post_tap1_max	1	(normalized)					
f_z	42.50	GHz		BREAD_CRUMBS	1	logical	f_fe_tapn_max	1	(normalized)		FV-LMS or MMSE			
f_p1	42.50	GHz					FFE_OPT_METHOD	MMSE						
f_p2	106.25	GHz					num_ui_RXFF_noise	1024			FOM or ISI			
g_DC_HP	-4		[min:step:max]				RXFFE_FLOAT_CTL	FOM						
f_HP_DZ	1.328125	GHz		Floating Tap Control			N_bg	2	0 1 2 or 3 groups					
Butterworth	1	logical	include in fr	baseline			N_bf	4	taps per group					
				new			N_f	50	UI span for floating taps					
				relevant for RxFFE			bm_avg	0.2	max DFE value for floating taps					
				adjusted in experiment			B_float_RSS_MAX	1	RSS tail tap limit					
							N_tail_start	13	(UI) start of tail taps limit					